

# Methods to study the evolution of tree and stand variables over time

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# ■ Summary

## ■ Where do we get the data for growth studies?

→ Permanent and Interval plots

→ Temporary plots

→ Experimental trials

→ Continuous forest inventory data

→ Stem analysis

- Partial - analysis of increment cores at dbh level
- Total - analysis of several tree discs along the stem

▪ **Where do we get the data for growth studies?**

# Where do we get the data for growth studies?

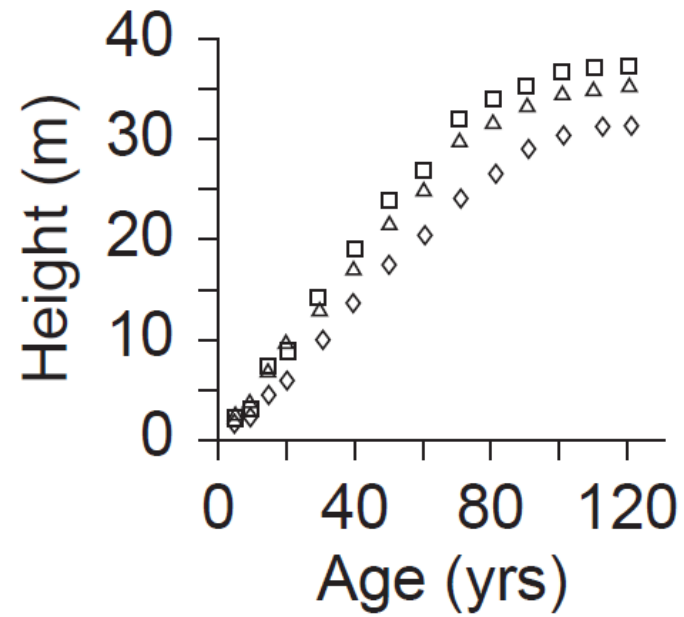
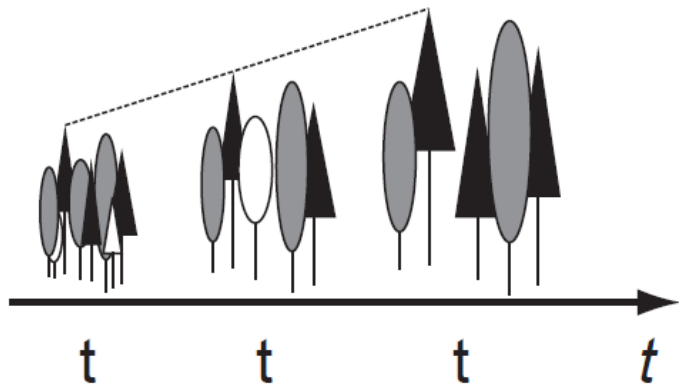
## ■ In permanent and interval plots

- Plots established with the objective of measuring growth in stands managed according to “current” practices
  - Permanent plots follow the stand during a long period, eventually the whole life of the stand

## ■ Permanent plots

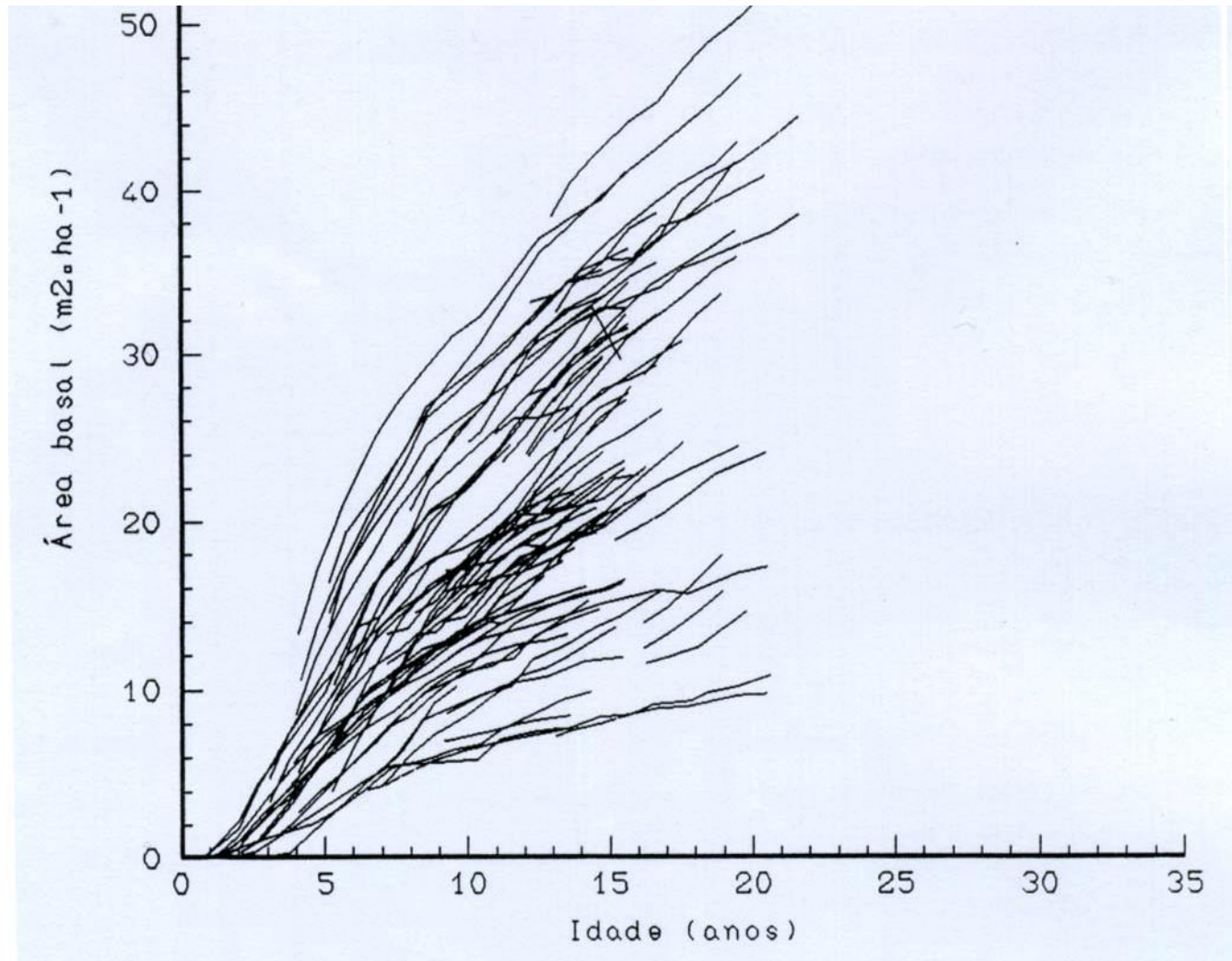
- Permanent plot with three successive measurements (white trees are removed during thinning). Graphical representation of data series of three permanent plots

(a)



## ■ Permanent plots

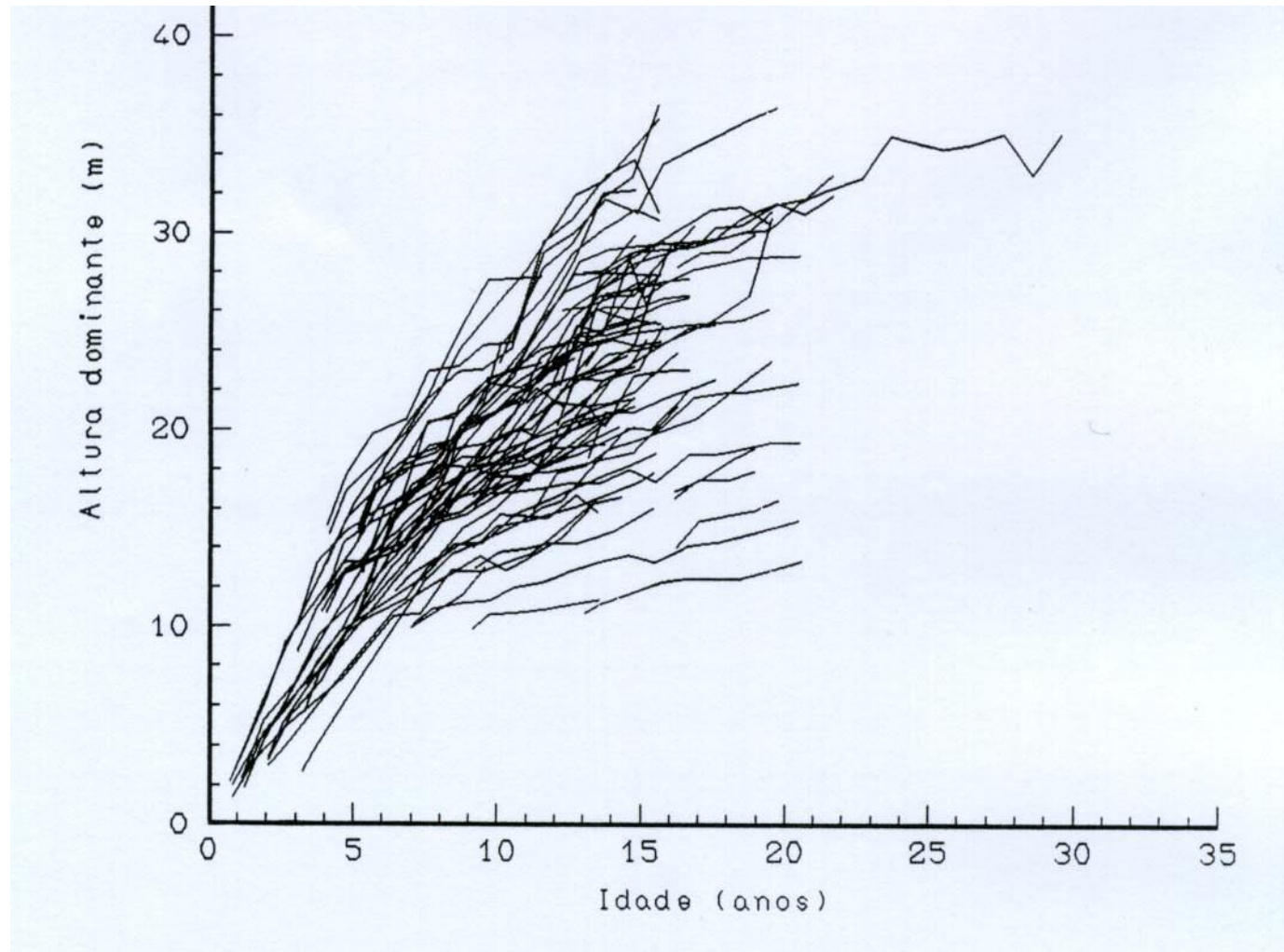
Examples of  
permanent plot  
data  
G - eucalyptus



## ■ Permanent plots

Examples of  
permanent plot  
data

$h_{dom}$  - eucalyptus



# Where do we get the data for growth studies?

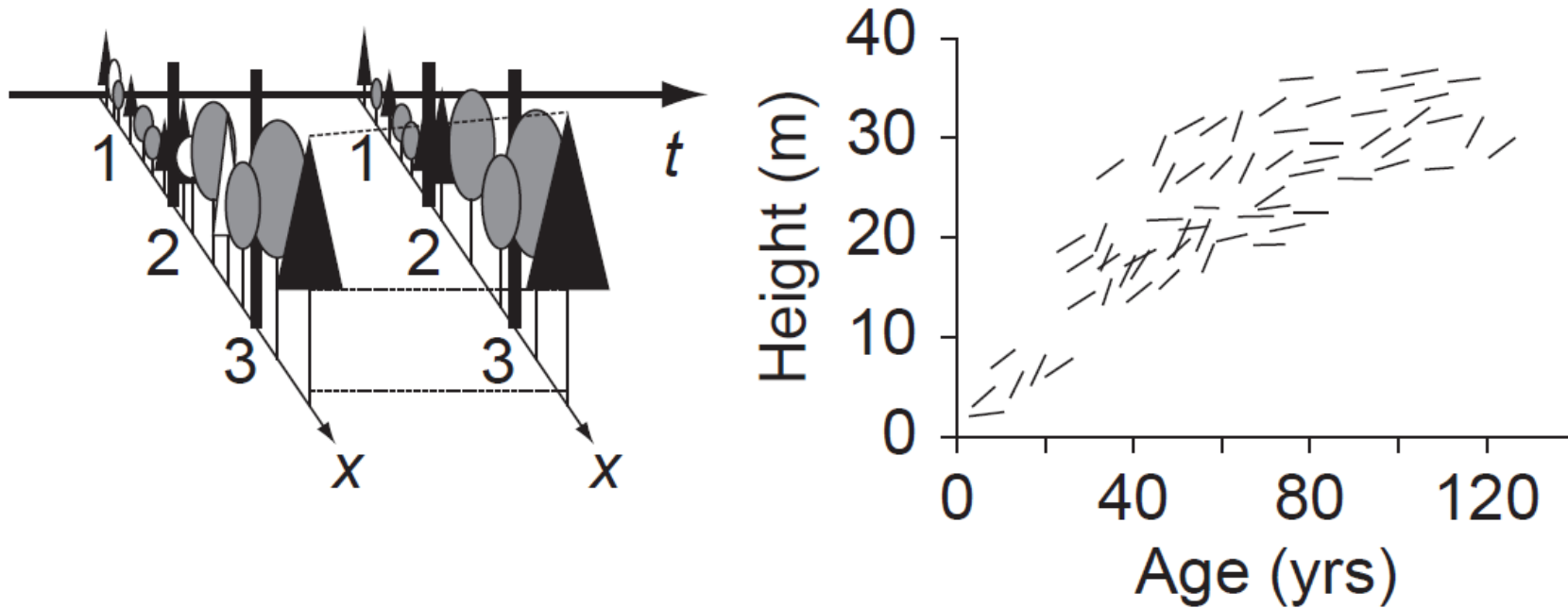
## ■ In permanent and interval plots

- ➔ Plots established with the objective of measuring growth in stands managed according to “current” practices
  - Permanent plots follow the stand during a long period, eventually the whole life of the stand
  - Interval plots follow the stand during a limited interval, but they are remeasured at least once



## Interval plots

- Three interval plots measured twice (white trees removed in thinning operations). Graphical representation: interval data for obtaining rates of change of observed state variables



# Where do we get the data for growth studies?

## ■ In permanent and interval plots

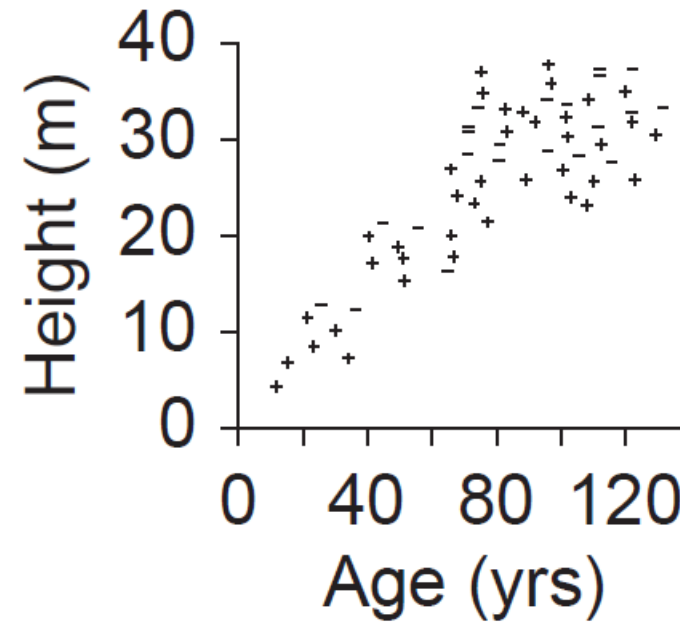
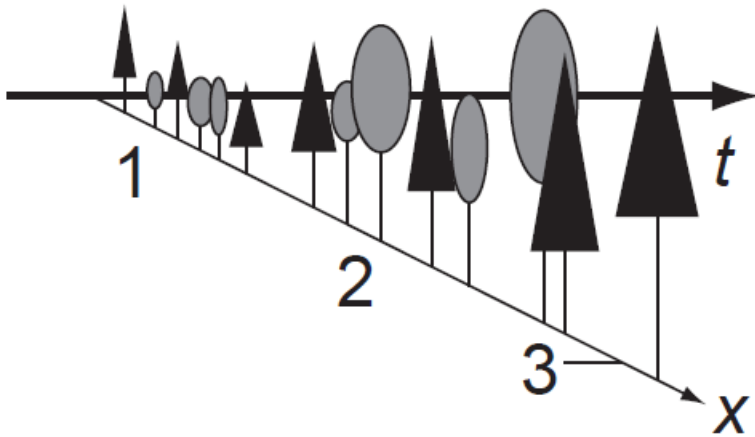
- Plots established with the objective of measuring growth in stands managed according to “current” practices
  - Permanent plots follow the stand during a long period, eventually the whole life of the stand
  - Interval plots follow the stand during a limited interval, but they are remeasured at least once

## ■ In temporary plots

- Plots that are measured just at one point in time

# ■ Temporary plots

- Three temporary plots of varying age (white trees removed in thinning operations). Graphical representation: independent height-age data obtained from temporary plots

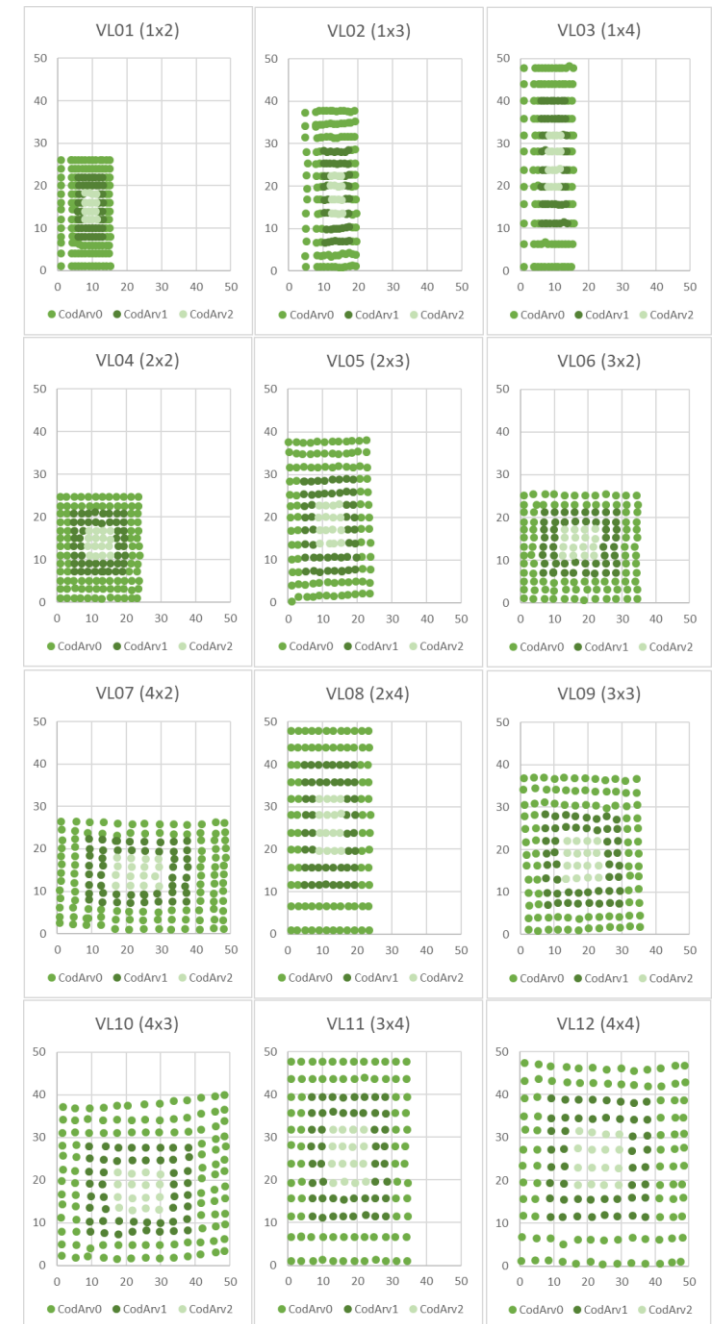
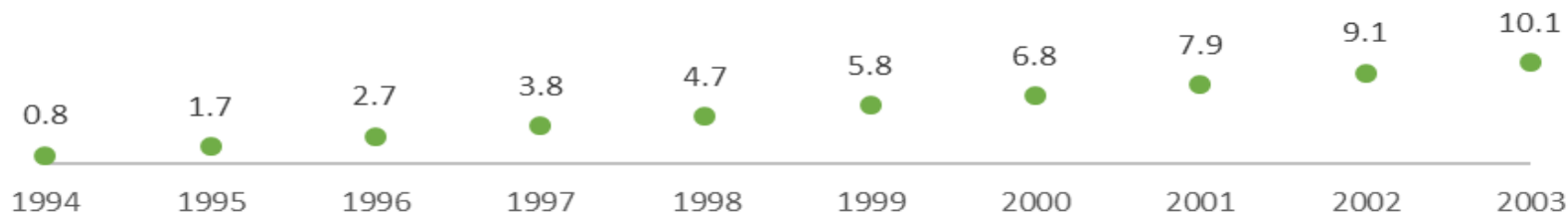


## Where do we get the data for growth studies?

- In designed silviculture and genetic trials
  - Trials purposively established to study the impact of silvicultural treatments and/or genetic material on tree and stand growth
- From continuous forest inventory data
- From stem analysis

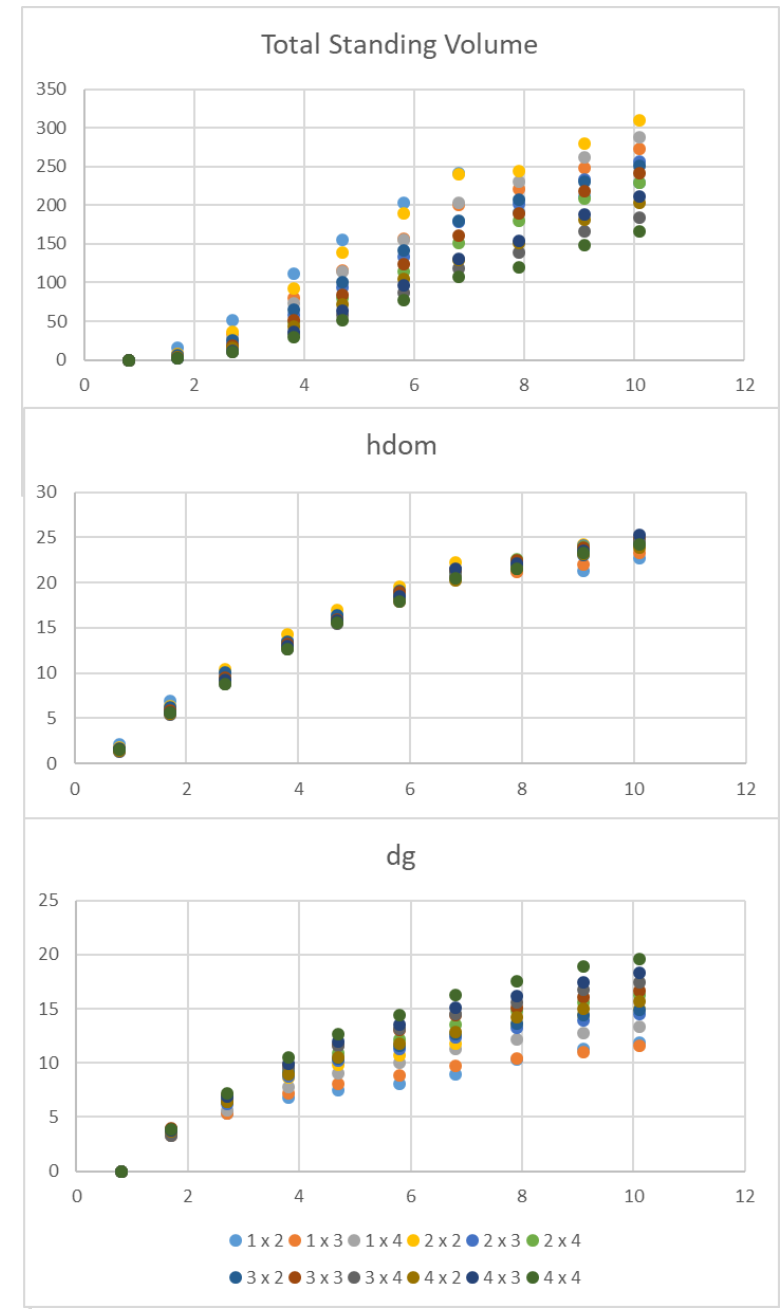
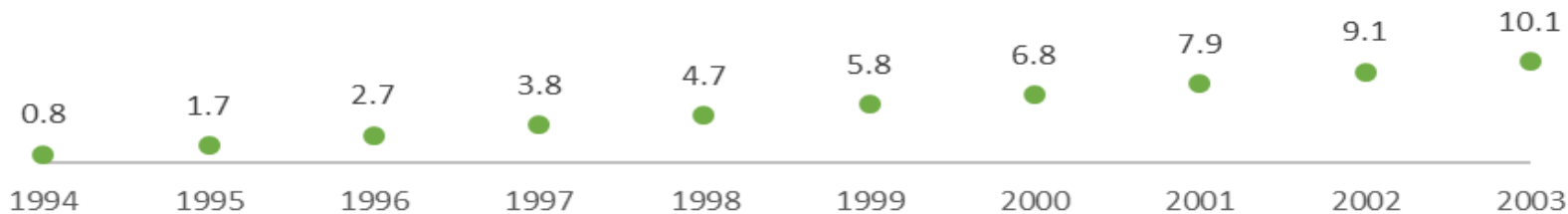
# Experimental trials

- ✓ Trials are set to study one specific silvicultural practice or a combination of two even if in practice several treatments are applied simultaneously
- ✓ Trials usually present a design with repetitions of the given treatment
- ✓ E.g Spacing trial: (1x2, 1x3, 1x4, 2x2, 2x3, 3x2, 4x2, 2x4, 3x3, 4x3, 3x4, 4x4) \* 3Blocks
- ✓ Measurements over time covering the entire 1<sup>st</sup> rotation



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## ■ Experimental trials

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- ✓ Comparison of some stand variables at age 10.1:

	5000	3333	2500	2500	1667	1667	1250	1250	1111	833	833	625
	1 x 2	1 x 3	1 x 4	2 x 2	2 x 3	3 x 2	2 x 4	4 x 2	3 x 3	3 x 4	4 x 3	4 x 4
ddom	18.60	18.02	20.75	21.48	20.63	20.80	22.04	22.25	22.02	23.00	24.83	24.79
dg	11.90	11.53	13.33	15.00	14.50	14.90	16.23	15.70	16.70	17.40	18.30	19.60
hdom	22.70	23.30	24.21	24.60	24.69	24.23	24.67	23.88	24.91	24.63	25.34	24.29
N	2734	2604	2018	1797	1502	1406	1042	1061	1024	746	742	534
V	229.08	272.73	288.21	309.32	256.19	229.04	251.53	240.96	184.10	202.42	211.14	165.75

**ANALYSIS OF MEASURED RESULTS**

**PERMANENT PLOTS**

**FIELD TRIALS**

Data for  
construction and  
validation

Indication for the  
need to obtain new  
data

Better  
understanding of  
physiological  
processes

Ideas for new  
experiments

**ANALYSIS OF SIMULATED RESULTS using  
FOREST GROWTH MODELS**

Better understanding of  
physiological  
processes

**EXPERIMENTS  
UNDERTAKEN IN  
LABORATORY**



## ■ Stem analysis

- Stem analysis is the study of tree growth from the analysis and measurement of the growth rings
- It is restricted to the species whose wood exhibits clear growth rings and to the regions with a climate that implies a clear stop on growth
- Two types of stem analysis:
  - Partial - analysis of increment cores at dbh level
  - Total - analysis of several tree discs along the stem

# Partial stem analysis

## Stand table projection

- It is usually used for short term projections of forest inventory data:
  1. During the forest inventory an increment core is taken in some “sample” trees
  2. Diameter growth of wood in the last  $k$  years (usually 5 years) is measured in the increment bore from each tree and converted to diameter growth
  3. Estimate the diameter growth ( $id_j$ ) of the average tree of each diameter class ( $j$ )



# Partial stem analysis

## Stand table projection

- It includes several steps *(and assumes you have just completed your forest inventory)*:
  1. Start by computing the stand table (number of trees per diameter class) from forest inventory data
  2. Estimate mortality in each diameter class and compute the future number of trees
  3. Compute the **growth index** or ratio between  $id_j$  and the width of the class - this index allows the computation of the number of trees that stay in the class and the ones that move 1 or 2 classes
    - A  $GI=0.76$  means that 76% of the trees move 1 class and none move 2 classes
    - A  $GI=1.10$  means that 90% of the trees move 1 class and 10% move 2 classes

Where  $id_j$  is the increment in diameter

# Partial stem analysis

## Stand table projection

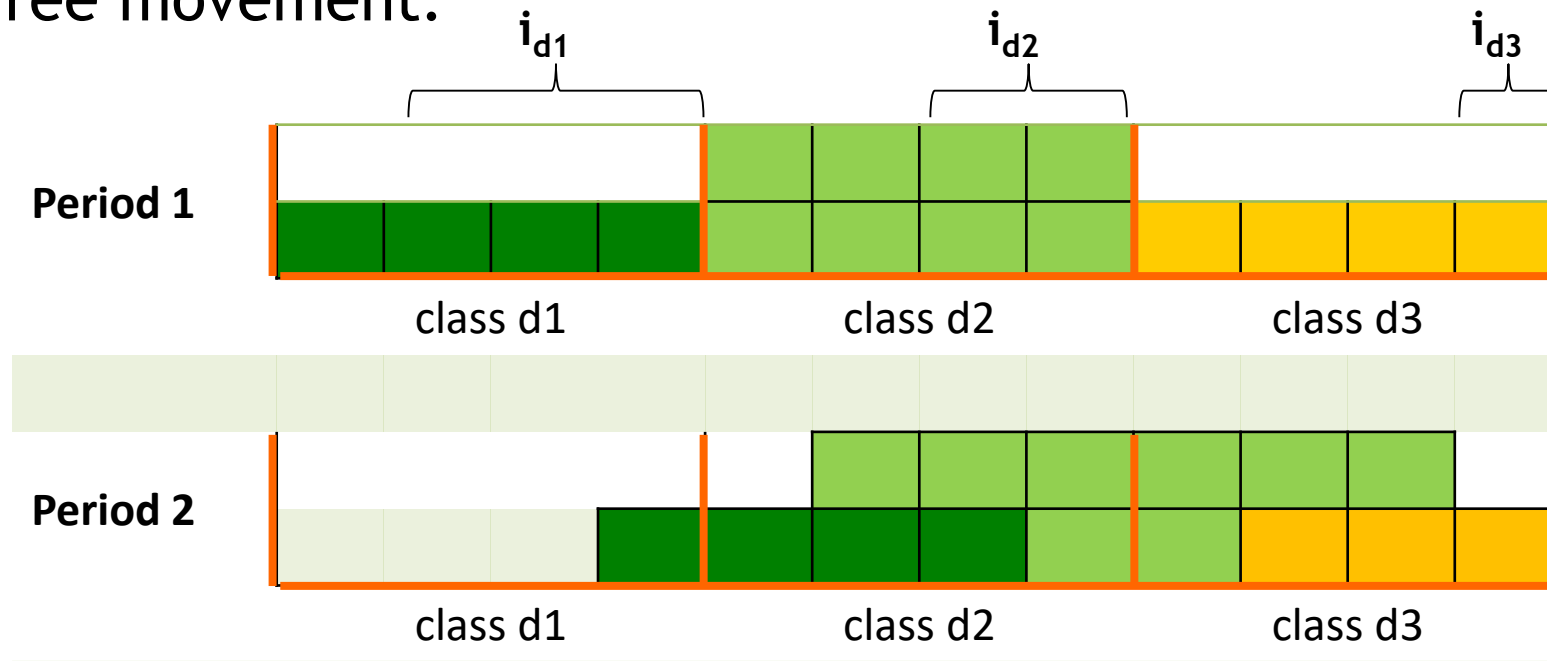
### ■ Computation of **growth index**:

- Assumes that trees inside a dbh class have a uniform distribution
- Estimate the diameter increment in  $k$  years of each dbh class ( $i_d$ )
- All trees inside a dbh class  $[d_1; d_2[$  with  $d > d_2 - i_d$ , after  $k$  years will be in the next class

# Partial stem analysis

## Stand table projection

### ■ Tree movement:



→ Note that now the trees are not equally distributed but this assumption will hold for the next period projection

# Partial stem analysis

## Stand table projection

class j (5 cm)	N <sub>j1996</sub> after mortality	d increment id <sub>5</sub> (cm)	Growth index		Movements			N <sub>j2001</sub>
			P <sub>1</sub>	P <sub>2</sub>	stay	1 class	2 classes	
ingrowth						100		
5	102	3.80	0.76	0	24.48	77.52	0	
10	59	3.80	0.76	0	14.10	44.84	0	
15	53	3.85	0.77	0	12.21	40.81	0	
20	59	3.85	0.77	0	12.21	45.42	0	
25	58	3.85	0.77	0	12.21	45.42	0	
30	22	3.90	0.78	0	4.84	17.16	0	
35	1	3.90	0.78	0	0.22	0.78	0	
40	0							
45								
Total								

=3.80/5cm

=102-24.48

=102\*(1-0.76)

Future number of trees alive in each class

Increment in diameter for the period

# Partial stem analysis

## Stand table projection

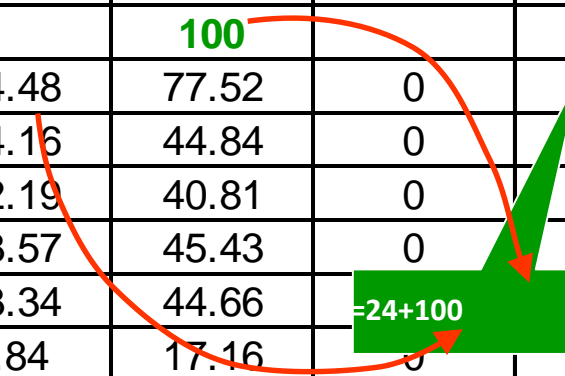
- We should also take into account the ingrowth
  - trees that achieve the lower limit of the first diameter class and must be added to the stand

# Partial stem analysis

## Stand table projection

class j (5 cm)	N <sub>j1996</sub> after mortality	d increment id <sub>5</sub> (cm)	Growth index		Movements			N <sub>j2001</sub>
			P <sub>1</sub>	P <sub>2</sub>	stay	1 class	2 classes	
ingrowth						100		
5	102	3.80	0.76	0	24.48	77.52	0	124
10	59	3.80	0.76	0	14.16	44.84	0	92
15	53	3.85	0.77	0	12.19	40.81	0	57
20	59	3.85	0.77	0	13.57	45.43	0	54
25	58	3.85	0.77	0	13.34	44.66	0	59
30	22	3.90	0.78	0	4.84	17.16	0	50
35	1	3.90	0.78	0	0.22	0.78	0	17
40	0							1
45								
Total	354							454

=24+100





# Partial stem analysis

## Stand table project

- To estimate volume (or biomass) increment:
  - Estimate the height of the average tree in each diameter class using a height-diameter curve
  - Estimate the respective volume with a volume equation
  - Estimate the volume in each point in time using the stand tables
  - Obtain the volume (biomass) growth by difference

# Partial stem analysis

## Stand table projection

class j (5 cm)	N <sub>j1996</sub> after mortality	N <sub>j2001</sub>	h <sub>j</sub> m	v <sub>j</sub> m <sup>3</sup> /tree	V <sub>j1996</sub> m <sup>3</sup> /ha	V <sub>j2001</sub> m <sup>3</sup> /ha
ingrowth						
5	102	124	6.8	0.0070	0.71	0.87
10	59	92	12.1	0.0470	2.77	4.30
15	53	57	16.2	0.1387	7.35	7.91
20	59	54	19.7	0.2939	17.34	15.98
25	58	59	22.5	0.5204	30.18	30.58
30	22	50	24.9	0.8237	18.12	40.77
35	1	17	27.0	1.2080	1.21	20.99
40	0	1	28.7	1.6763	0.00	1.31
45						0
Total	354	454			78	123

=0.0070\*124

V growth  
m<sup>3</sup>/ha

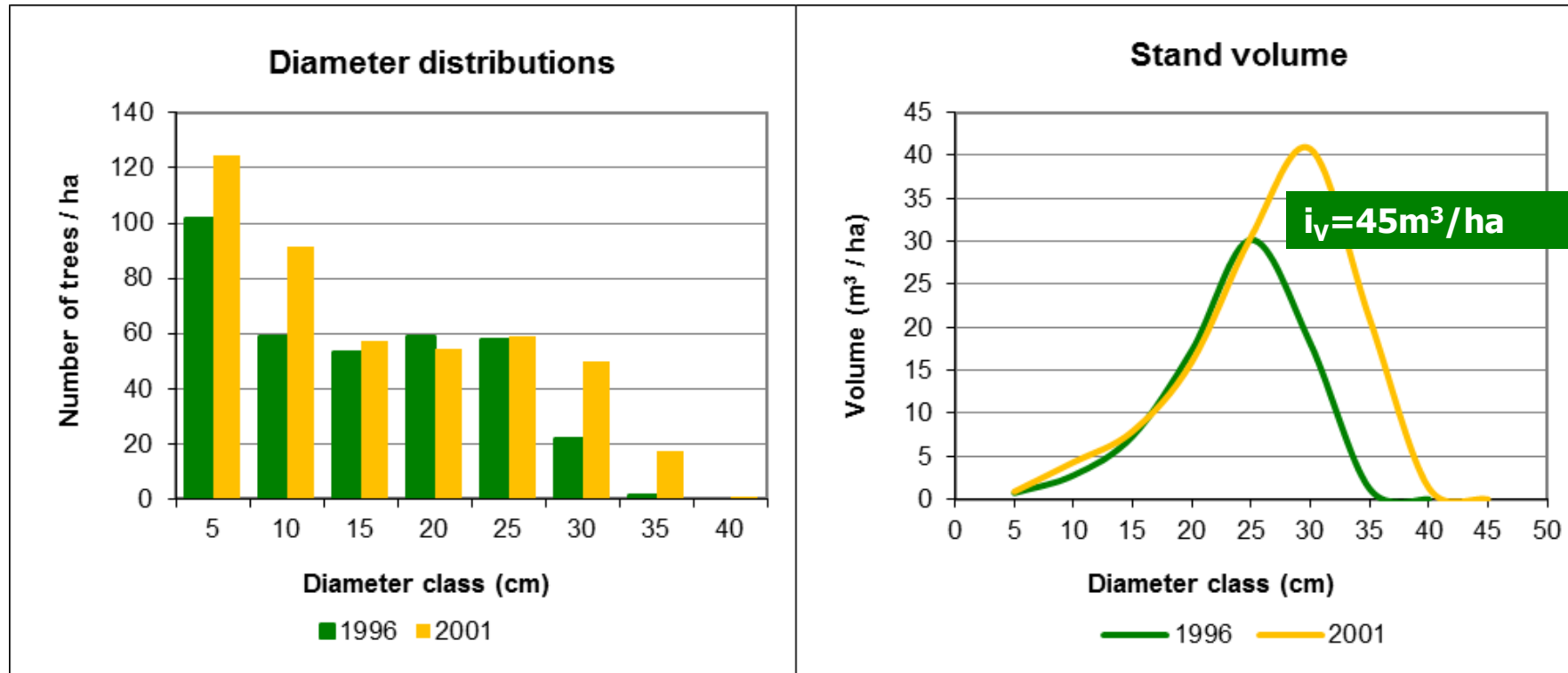
45

Tree height with a height-diameter curve:  $h = d / (0.64212 + 0.01874 * d)$

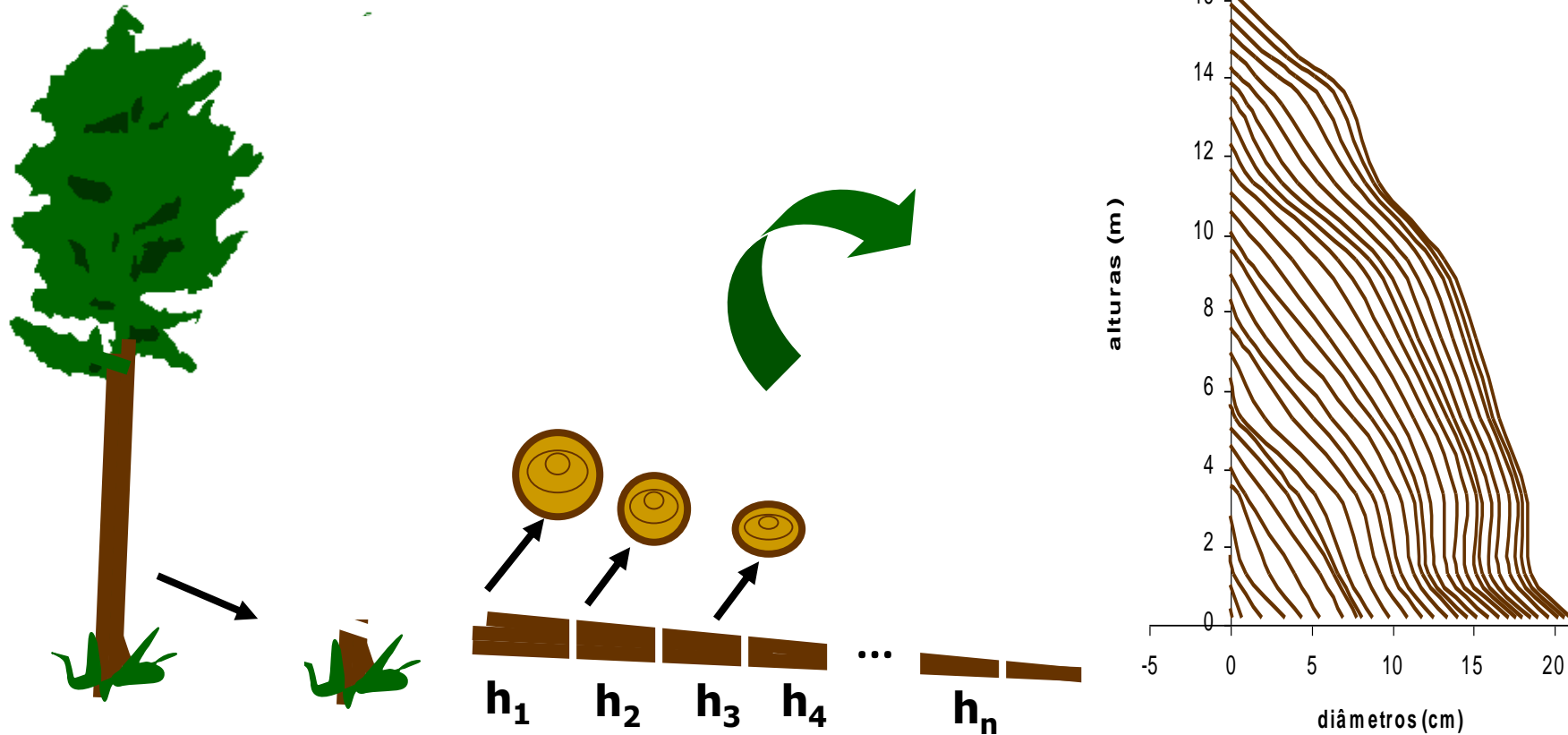
Total volume with a volume equation:  $v = 0.00005126 d^{2.0507} h^{0.8428}$

# Partial stem analysis

## Stand table projection



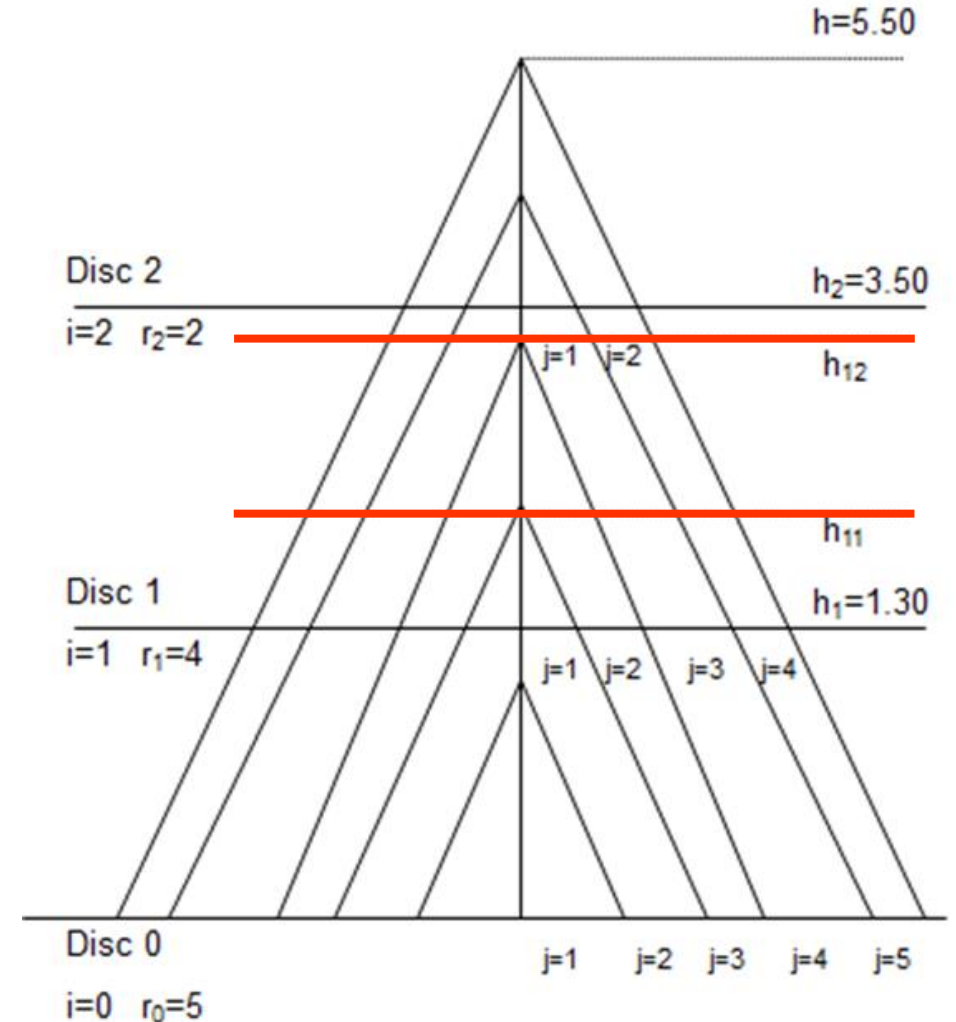
# Total stem analysis



# Stem analysis - example

height	N rings	age
0	5	0
1.30	4	1+ ...
3.50	2	3+ ...
5.50	0	5

- ✓ Tree is 5 years old
- ✓ Between Disc 1 and Disc 2, the correction is needed to estimate the heights at the end of the years:  $h_{11}$  and  $h_{12}$
- ✓ The method most used for this correction is the Carmean method



# Stem analysis

## Carmean's correction

- Carmen's method is based on two assumptions:
  1. Constant annual increment in height between two discs
  2. Each disc occurs at the mid-point between two whorls
- The application of the method to the whorls between two discs implies:
  - ➔ Computing the annual increment  $i_h = (h_2 - h_1) / (nrg_1 - nrg_2)$ , where  $h_i$  and  $nrg_i$  are the height and the number of rings of disc<sub>*i*</sub>
  - ➔ Computing the height of the first whorl as:  $h_{i1} = h_i + i_h / 2$
  - ➔ Computing the height of the remaining whorls as:  $h_{ij} = h_i + i_h / 2 + (j-1) * i_h = h_{i(j-1)} + i_h$

# Stem analysis

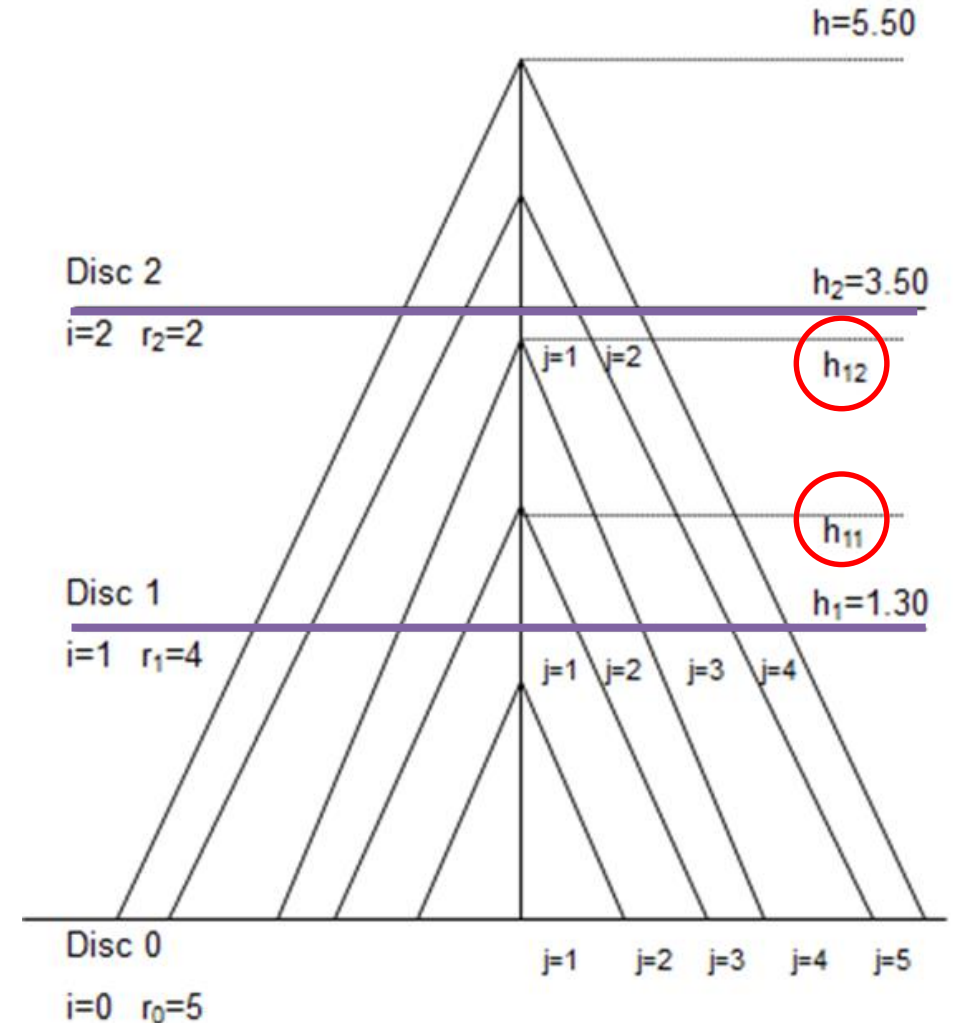
## Carmean's correction

Let's compute  $h_{11}$  and  $h_{12}$ :

✓ Annual height growth **between discs**:

$$i_h = (h_2 - h_1) / (nrg_1 - nrg_2)$$

$$i_h = (h_2 - h_1) / (4 - 2) = (3.50 - 1.30) / 2 = 1.1$$



# Stem analysis

## Carmean's correction

Let's compute  $h_{11}$  and  $h_{12}$ :

✓ Annual height growth:

$$i_h = (h_2 - h_1) / (nrg_1 - nrg_2)$$

$$i_h = (3.50 - 1.30) / (4 - 2) = 1.1$$

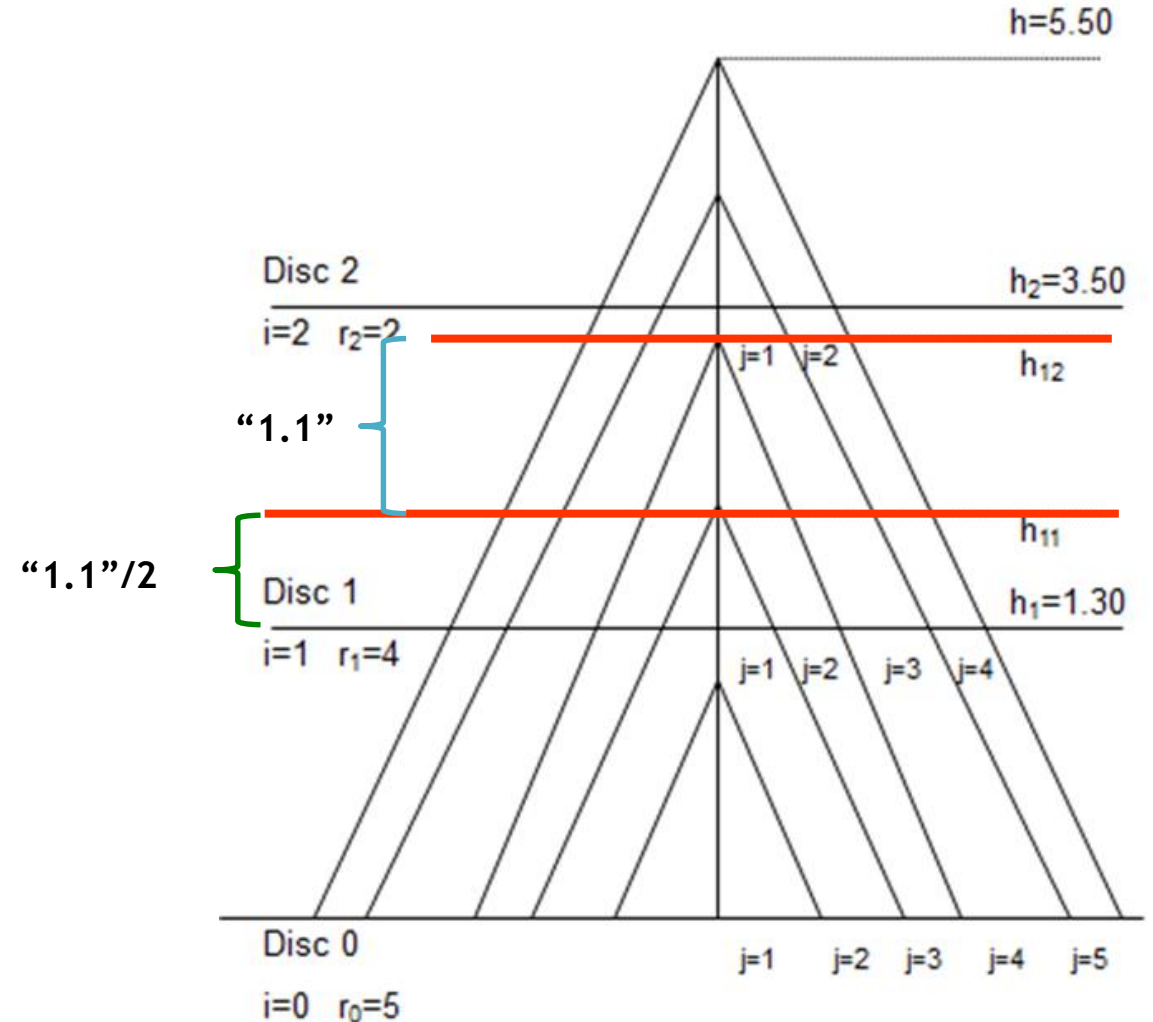
$$h_{i1} = h_i + i_h / 2$$

$$h_{11} = 1.30 + 1.1 / 2 = 1.85$$

$$h_{ij} = h_i + i_h / 2 + (j-1) * i_h = h_{i(j-1)} + i_h$$

$$h_{12} = h_{11} + i_h = 1.85 + 1.1 = 2.95$$

Where  $nrg_1$  and  $nrg_2$  are the number of rings in the discs collected at heights 1 and 2 respectively.





# Stem analysis

## Carmean's correction

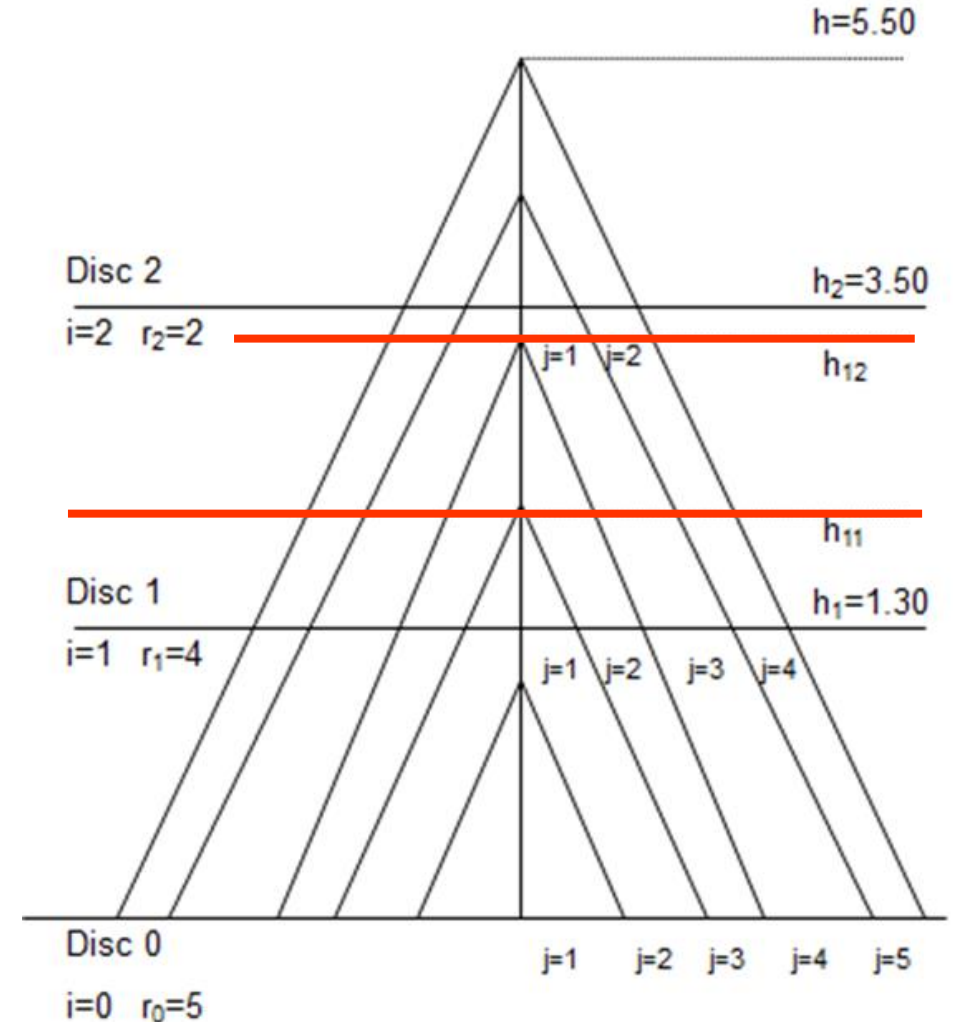
- It is possible to obtain a general formula for the height of any whorl  $h_{ij}$ :

$$h_{ij} = h_i + \frac{1}{2} \frac{h_{i+1} - h_i}{r_i - r_{i+1}} + (j-1) \frac{h_{i+1} - h_i}{r_i - r_{i+1}}$$

$\frac{h_{i+1} - h_i}{r_i - r_{i+1}}$  is the annual growth between discs  $i$  and  $i+1$

$$h_{11} = 1.30 + \frac{1}{2} \frac{3.50 - 1.30}{4 - 2} + (1-1) \frac{3.50 - 1.30}{4 - 2} = 1.30 + \frac{1}{2} 1.10 = 1.30 + 0.55 = 1.85$$

$$h_{12} = 1.30 + 0.55 + (2-1) 1.10 = 2.95$$



# Stem analysis

## Carmean's correction

