



# Forest Models Tipology

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# ■ Summary

- Forest growth models evolution
- Typology of forest growth models
  - ✓ Classification based on the **essence of the growth module** (empirical, process-based,...)
  - ✓ Classification based on the **unit of simulation** (individual tree, stand,...)
  - ✓ Classification based on the “**variability of outputs**” (deterministic, stochastic...)

# ▪ Forest growth models evolution

Forestry and forest management evolution



Increased knowledge about ecosystems functioning



Technology development



Climate change



Change in society requirements from forests



**EVOLUTION OF FOREST GROWTH MODELS**

# Empirical growth models

Incorporation of knowledge about the physiological processes



Flexibility and extrapolation ability

Yield tables (XIX century)

Stand models without d distribution (40's)

Stand models with d distribution (80's)

Individual tree models  
distance independent (80's)

Individual tree models  
distance dependent (80's)

**Combination of empirical and  
physiological models (2000)**

Physiological models  
"top-down" (80's)

**Process-based  
models**

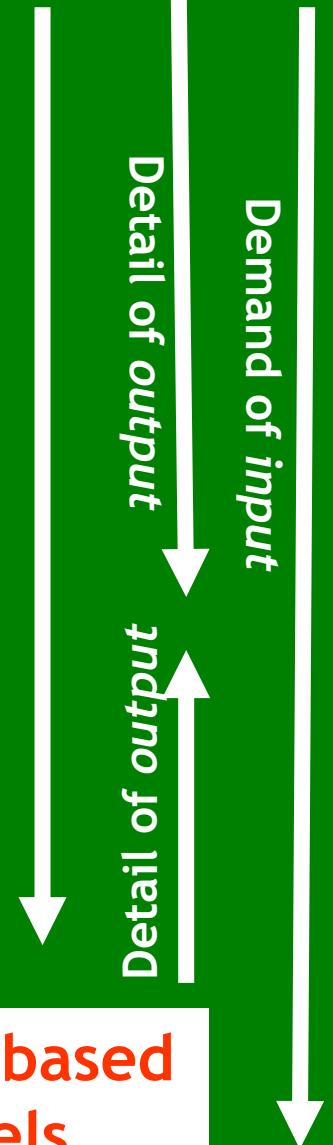
Structural complexity

Flexibility and extrapolation ability

Detail of output

Detail of input

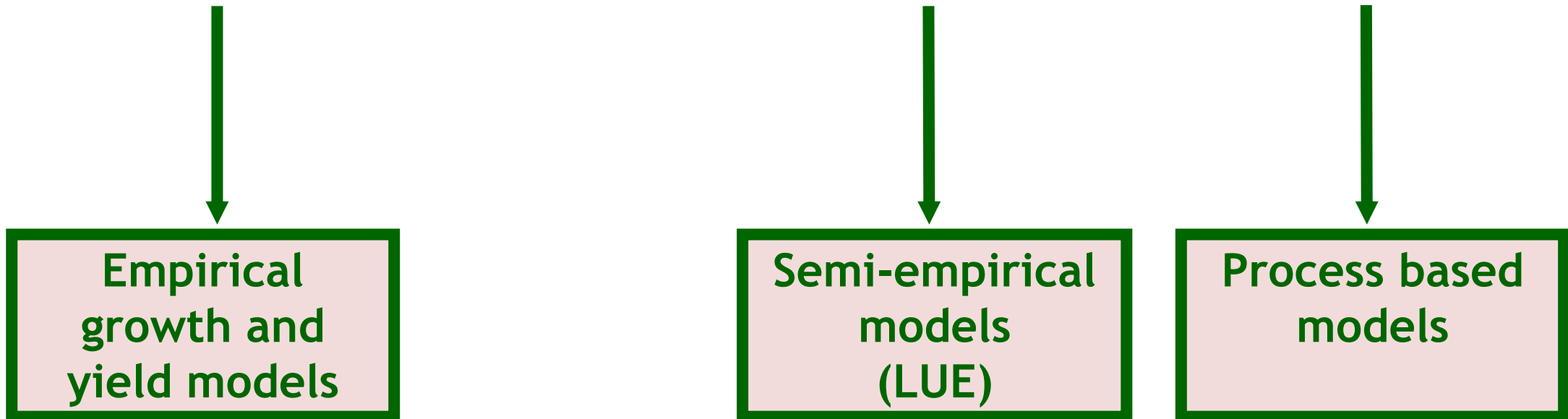
Demand of input



## ▪ Typology of forest growth models

# Forest growth models

Classification according to the growth module  
(to be used in practice all models need a static module)



**3PG**  
**YieldSAFE**

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## ▪ Statistical FGMs (empirical G&Y)

- ✓ Developed using statistical techniques and calibrated for large data-sets
- ✓ The site index (hdom at a given base-age) is often used as a proxy for environmental conditions
- ✓ Growth is usually modeled with the so-called **growth functions**
- ✓ Adequately describe growth for a range of silvicultural practices and site conditions
- ✓ Some are able to predict wood quality properties
- ✓ Exist for all of the most important forest types in Europe and most of them have been extensively validated
- ✓ Do not allow for the simulation of forest growth under a changing environment or subject to novel silvicultural practices



# The G&Y model GLOBULUS (empirical)

**Table 1.** Site Index and dominant height projection functions.

## Site Index and Dominant height

**Table 2.** Basal area: initialization function (1) and growth projection function (2).

## Basal Area

(1)  $SI = \dots$

$$(1) G = A_G e^{-k_G \left(\frac{1}{t}\right)^{n_{Gp} + 1}}$$

model

(1) and (2)

Where SI is the site index (tp=10 for eucalypt); 2 represent the ins

$$A_G = (a_{G0} + a_{G1} DR)$$

$$n_{Gp} = n_{G0} + \frac{n_{G1}}{\left(1 - \left(\frac{Cota}{2000}\right)^2\right)}$$

model	a <sub>G0</sub>	a <sub>G1</sub>	k <sub>G0</sub>
(1)	80.1683	0.2354	8.8294
(2)	80.1683	0.2354	-

Where G is the stand basal area; t (Symbols); SI is the site index; Cota is the stand rotation (0 for planted and 1 for coppice stands); DR is the dominant height ratio.

**Table 3.** Functions to predict the evolution of the number of trees, stumps and shoots

## Density and/or Mortality

**Table 4.** Volume initialization function (1) and Volume projection function (2),

### Planted Stands:

$$-am t$$

$$(1) N = N_{pl} e^{-am t}$$

$$-am (t_2 - t_1)$$

$$(2) N_2 = N_1 e^{-am (t_2 - t_1)}$$

$$(1) V_i = K_v t^a h_{dom}^c$$

### Coppice Stands:

$$(3) N_{stools} = N_{harv} (1 - dea)^{-t}$$

$$(2) V_{i2} = V_{i1} \left(\frac{t_2}{t_1}\right)^a \left(\frac{h_2}{h_1}\right)^c$$

$$(4) N_{stools_2} = N_{stools_1} e^{-\epsilon}$$

$$(5) N_{sprouts_{t \leq 2}} = N_{stools}^l$$

$$(6) N_{sprouts_{t=3}} = \frac{N_{stools}^l}{1 - e^{-ar}}$$

If there is any kind of sprouts selection, ar=1.6

model	a
(1) Vu	-0.0510
(2) Vu	-0.0511
(1) Vb	-0.0548
(2) Vb	-0.0548
(1) V_st	-0.0821
(2) V_st	-0.0821

## Volume Total

**Table 6.** Biomass prediction functions

## Biomass

$$W_i = a G^b h_{dom}^c$$

$$b = b_0 + b_1 \text{rot} + b_2 \left(\frac{N}{1000}\right) + b_3 \left(\frac{SI}{1000}\right) + b_4 \left(\frac{t}{1000}\right)$$

$$W_a = W_w + W_b + W_l + W_{br}$$

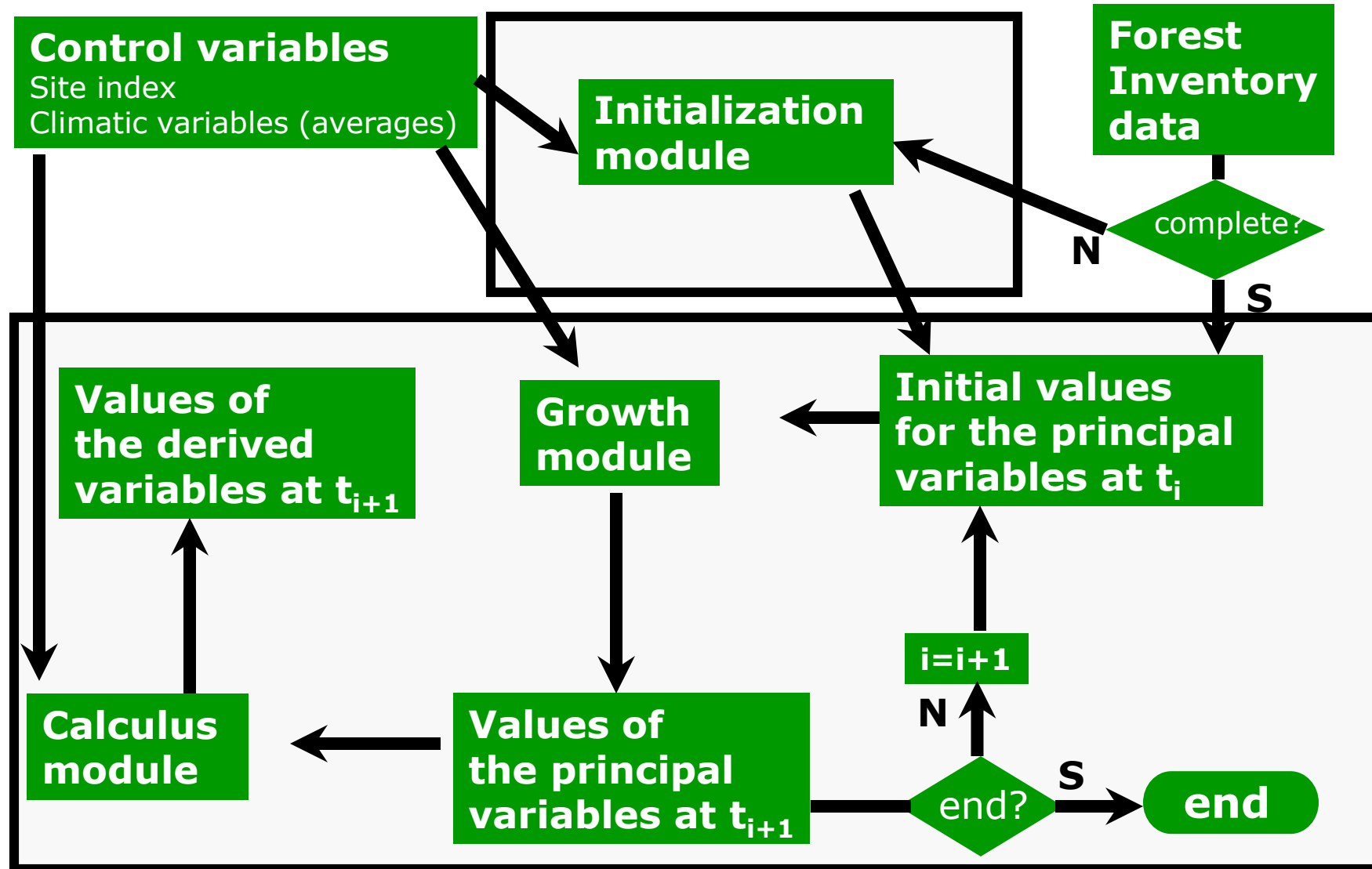
$$W_r = a W_a$$

$$W_t = W_a + W_r$$

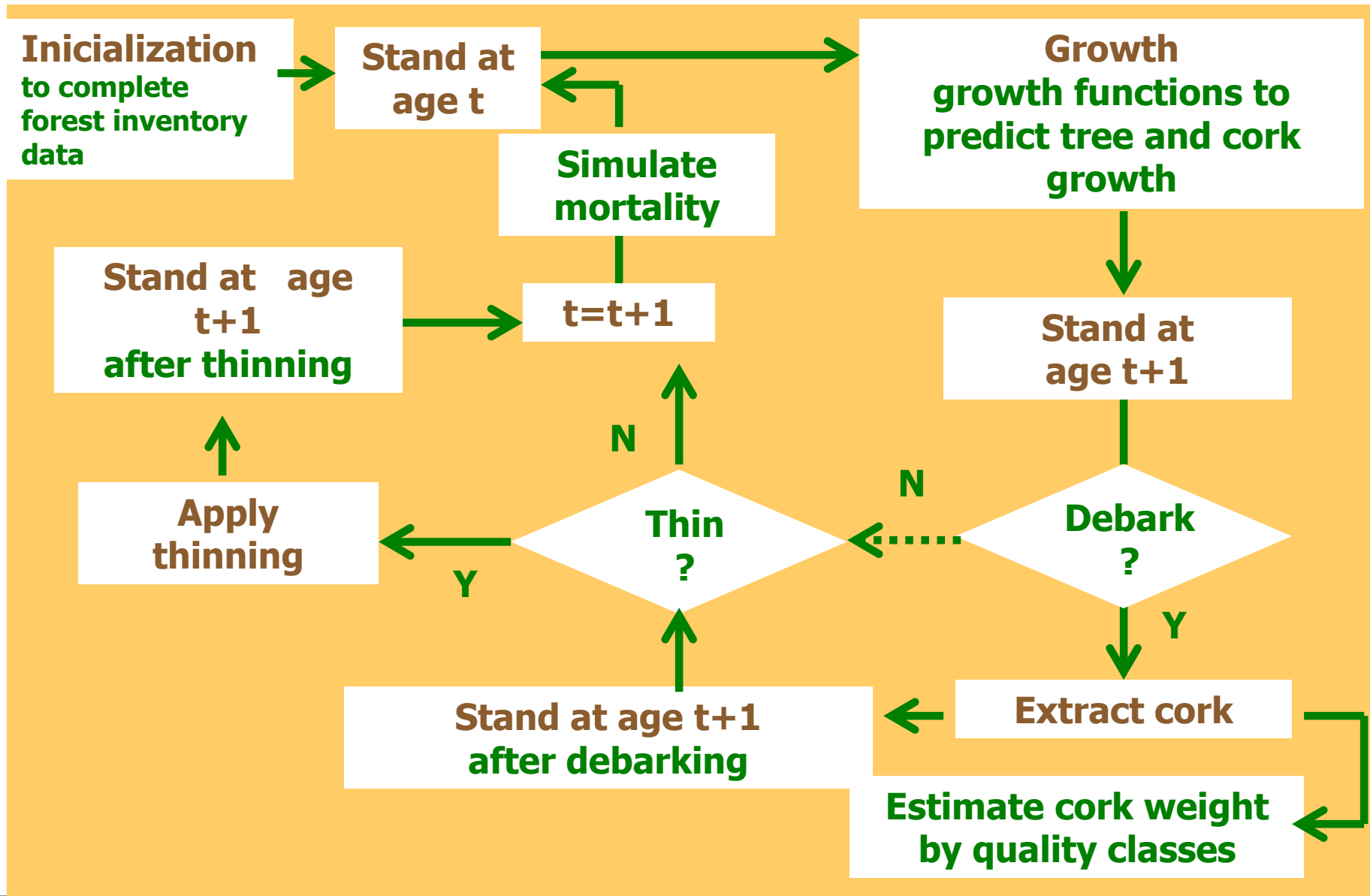
model	a	b <sub>0</sub>	b <sub>1</sub>	b <sub>2</sub>	b <sub>3</sub>	b <sub>4</sub>	c
W <sub>w</sub>	0.0967	1.0547	-0.0018	-0.0065	-0.5198	-1.2105	1.1886
W <sub>b</sub>	0.03636	1.1691	-0.0083	-0.0459	3.2289	2.0880	0.6710
W <sub>l</sub>	1.0440	1.0971	-	-0.0112	-1.2207	-6.2807	-0.3129
W <sub>br</sub>	0.3972	1.0005	-	-0.0192	3.3170	-1.2747	-0.0160
W <sub>r</sub>	0.2487	-	-	-	-	-	-

Where W<sub>i</sub> represents the following biomass components: W<sub>w</sub> is the biomass of wood, W<sub>b</sub> is the biomass of bark, W<sub>br</sub> is the biomass of branches and W<sub>l</sub> is the biomass of leaves; W<sub>a</sub> is the total aboveground biomass; W<sub>r</sub> is the biomass of roots; h<sub>dom</sub> is the stand dominant height; G is the stand basal area; SI is the site index; rot is the stand rotation (0 for planted and 1 for coppice stands); N is the stand density and

# LOBULUS - structure



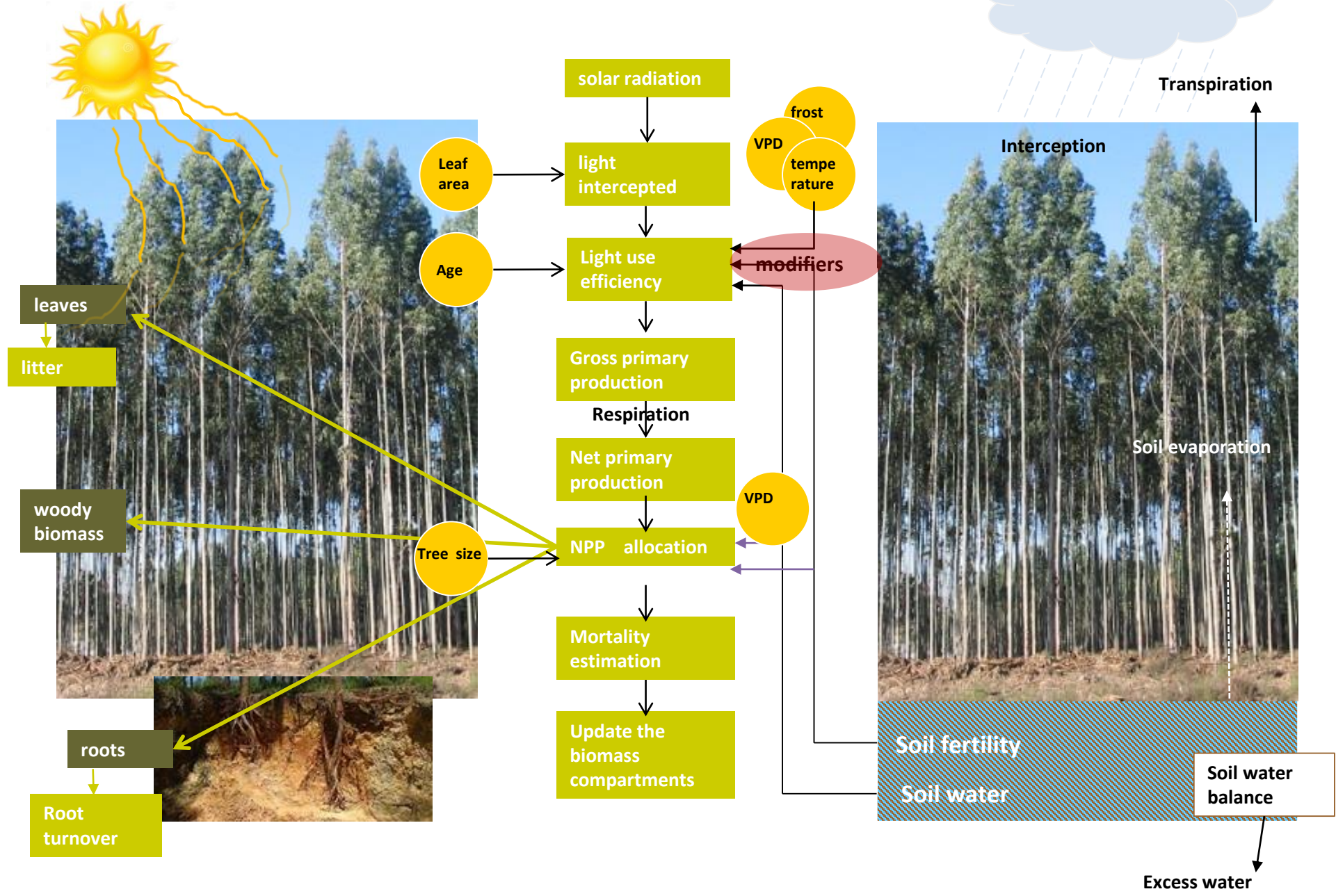
# SUBER model - structure



# Process-based ecophysiological models

- Developed to understand forest behavior from a description of plant-soil and carbon-nutrient-water interactions
- Allow the simulation of forest growth under a changing environment or subject to novel silvicultural practices
- The principal variables are biomass pools per tree component (leaves, branches, roots, wood)
- A specific problem with this type of model is the need for detailed input, demanding data which are rarely available at regional or lower levels
- Do not give all the output needed for forest management (but it can be easily added)

# 3PG model structure



# Growth modifiers in 3PG

- Each environmental factor is represented by a growth modifier or function of the factor that varies between 0 (total limitation) and 1 (no limitation)

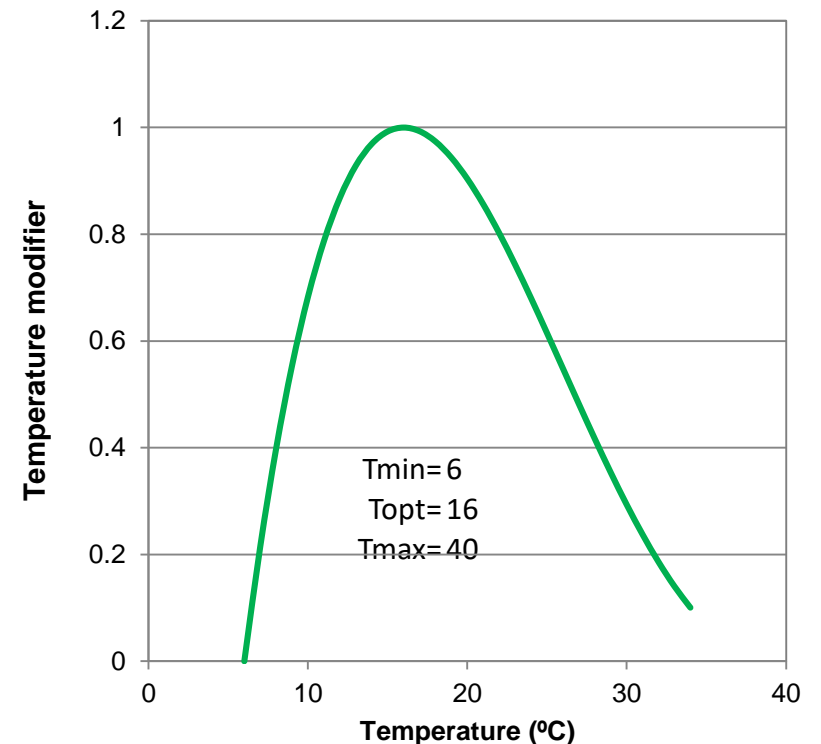
Factor	Modifier	Parameters
Vapor pressure deficit	$f_{VPD}(D)$	$k_D$
Soil water	$f_{SW}(\theta)$	$\theta_{max}, c_{\theta}, n_{\theta}$
Temperature	$f_T(T_{av})$	$T_{min}, T_{opt}, T_{max}$
Frost	$f_F(d_f)$	$k_F$
Site nutrition	$f_N(FR)$	$f_{N0}$
Stand age	$f_{age}(t)$	$n_{age}, r_{age}$

# An example: temperature growth modifier $f_T(T)$

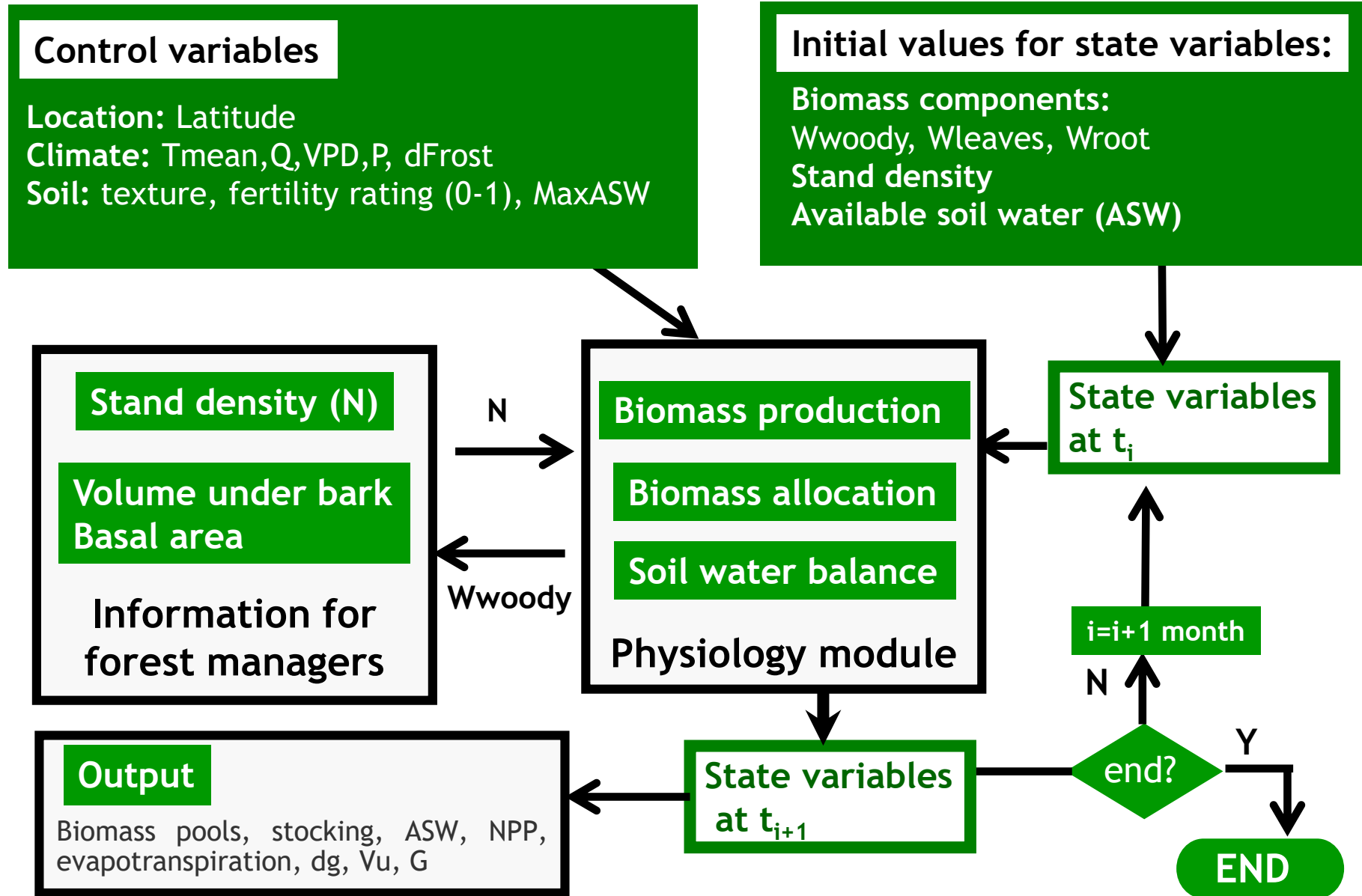
$$f_T(T) = \left( \frac{T - T_{min}}{T_{opt} - T_{min}} \right) \left( \frac{T_{max} - T}{T_{max} - T_{opt}} \right) \left( \frac{T_{max} - T_{opt}}{T_{opt} - T_{min}} \right)$$

where

- $T$  = mean monthly daily temperature
- $T_{min}$  = minimum temperature for growth
- $T_{opt}$  = optimum temperature for growth
- $T_{max}$  = maximum temperature for growth



# 3PG structure





# Hybridization

- Combination of different types of models/modelling methodologies, usually:
  - A process-based model (preferably not excessively input demanding) that:
    - is able to reflect the effect of climate changes
    - as well as the effect of management practices such as fertilization, irrigation, weeding ...
    - or the impact of pests and diseases
  - With empirical functions in order to obtain the same output as traditional growth and yield models (usually more detailed in what concerns stand and tree variables)

# Forest growth models

Classification according to the unit of simulation  
(growth module)



Stand models



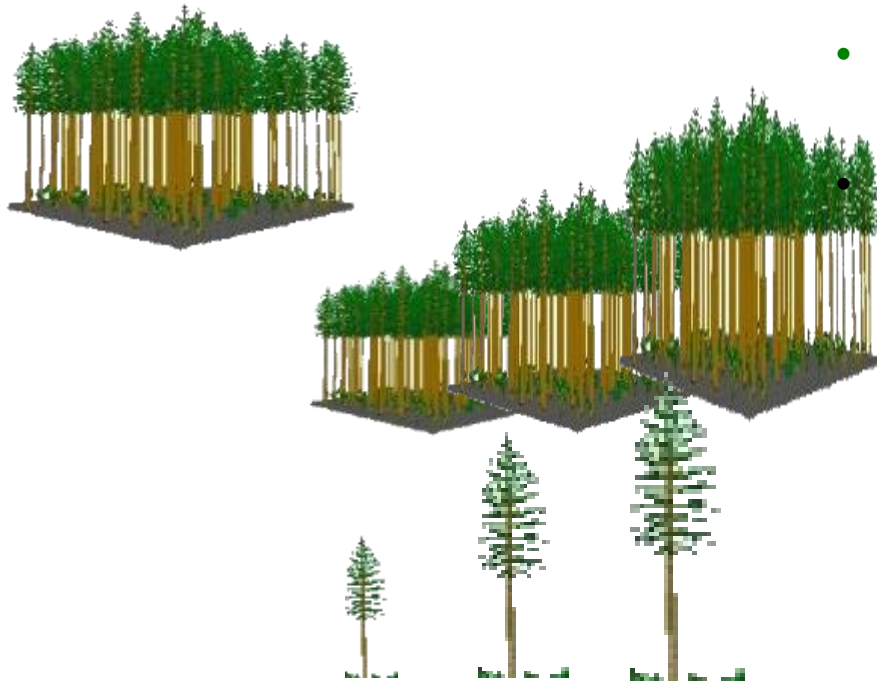
Stand models  
with simulation  
of the diameter  
distribution



Individual tree  
models

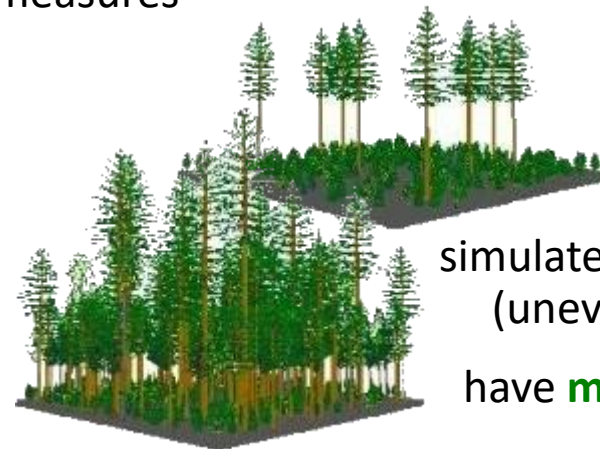
## Stand Model

- **Principal variables:**  
**stand** variables (all)
- **Competition:**  
stand density measures



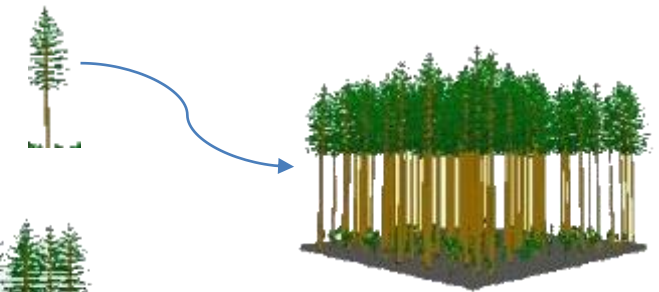
## Stand Model *with* Diameter Distribution

- **Principal variables:**  
**stand** variables  
(including the variables  
needed to simulate  
**diameter distribution**)
- **Volume and biomass**  
**computed from the dd**
- **Competition:**  
stand density measures



## Individual Tree Model

- **Principal variables:**  
**tree** variables (except hdom)
- **Competition (inter-tree):**
  - competition indices
  - light interception modules



simulate more **complex structures**  
(uneven-aged, mixed-stands)  
have **more extrapolation ability**

# ▪ Requirements from forest models - moving

## FROM

- ✓ Stand models
- ✓ Empirical models
- ✓ Stand simulators
- ✓ Simple structure forests
- ✓ Focusing just trees
- ✓ Simple output, mainly traditional stand variables and volume harvested

## TO

- ✓ Individual tree models
- ✓ Process based models
- ✓ Management unit simulators
- ✓ Complex forests (uneven and mixed)
- ✓ Focusing other ecosystem components (e.g shrubs, soils)
- ✓ Diversified output, including social, economic and ecological indicators

**Life is not easy for growth modelers!!**

## ▪ **Deterministic *versus* stochastic models**

- ✓ Provide an estimation of the **expected growth** in a stand, for certain initial conditions
- ✓ For the same initial conditions, the models always provides **the same prediction**
- ✓ Try to simulate the **variation** from the real world
- ✓ For the same initial conditions provides **different predictions** (as a function of its probability of occurrence)
- ✓ Gives additional information on the **variability** observed in growth

**The two types of models can be combined in the same simulator**