

# Solving applications of Linear Programming with Excel SOLVER

APPLIED OPERATIONAL RESEARCH

Susana Barreiro February 27

ISA - Applied Operational Research - 2024/2025



## Question 2.

#### Test - 25 May 2016

A farmer has the following resource endowments: 500 acres of land, 1500 hours of family labour and 120000 € of capital investment. She can use these resources to grow the following crops: corn, sorghum, wheat and soybeans. Any crop should not occupy more than 250 acres. Assume that the farmer works to maximize profit (revenue minus costs) from the production of these crops. She expects the following in terms of prices, crop yields, costs and labor requirements.

	Price	Yield	Cost	Labor Requirement
Crop	(€/bushel)	(bushel/acre)	(€/acre)	(hours/acre)
Corn	2.75	120	250	3.25
Sorghum	2.65	100	200	3.00
Wheat	3.15	105	245	3.15
Soybeans	6.75	45	230	3.30

- 1. Formulate the problem as a linear program.
- 2. Solve the problem using the Excel Solver. What is the optimal solution to the problem?
- 3. Which constraints are binding? How do you interpret each binding constraint?
- 4. By how much should sorghum's current profit per acre increase in order for the optimal solution to change? Sorghum's current profit per acre decrease would change the optimal solution?
- 5. What is the shadow price for each constraint? How do you interpret this value?
- 6. What is the range of feasibility for the maximum number of hours of family labour with respect to the shadow price? How do you interpret this range?
- 7. How much the profit would change if one acre of soybeans were forced into the current optimal solution?



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Soybeans	6.75	45	230	3.30

#### 1. Formulate the problem as a linear program.

$$\begin{array}{l} \text{Maximize} \mid Z = 80x_1 + 65x_2 + 85.75x_3 + 73.75x_4 \\ x_1 + x_2 + x_3 + x_4 \leq 500 \\ x_1 \leq 250 \\ x_2 \leq 250 \\ x_3 \leq 250 \\ x_4 \leq 250 \\ 3.25x_1 + 3.00x_2 + 3.15x_3 + 3.30x_4 \leq 1500 \\ 250x_1 + 200x_2 + 245x_3 + 230x_4 \leq 120000 \\ x_1, x_2, x_3, x_4 \geq 0 \end{array}$$



### Question 2.

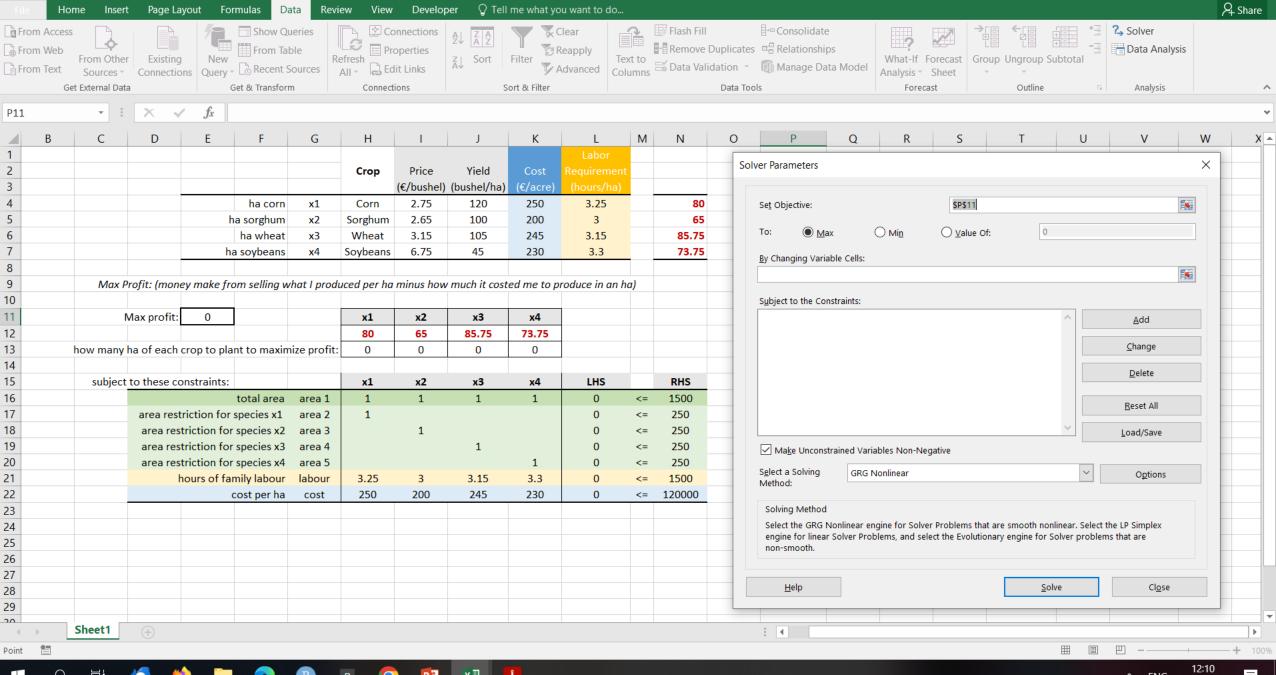
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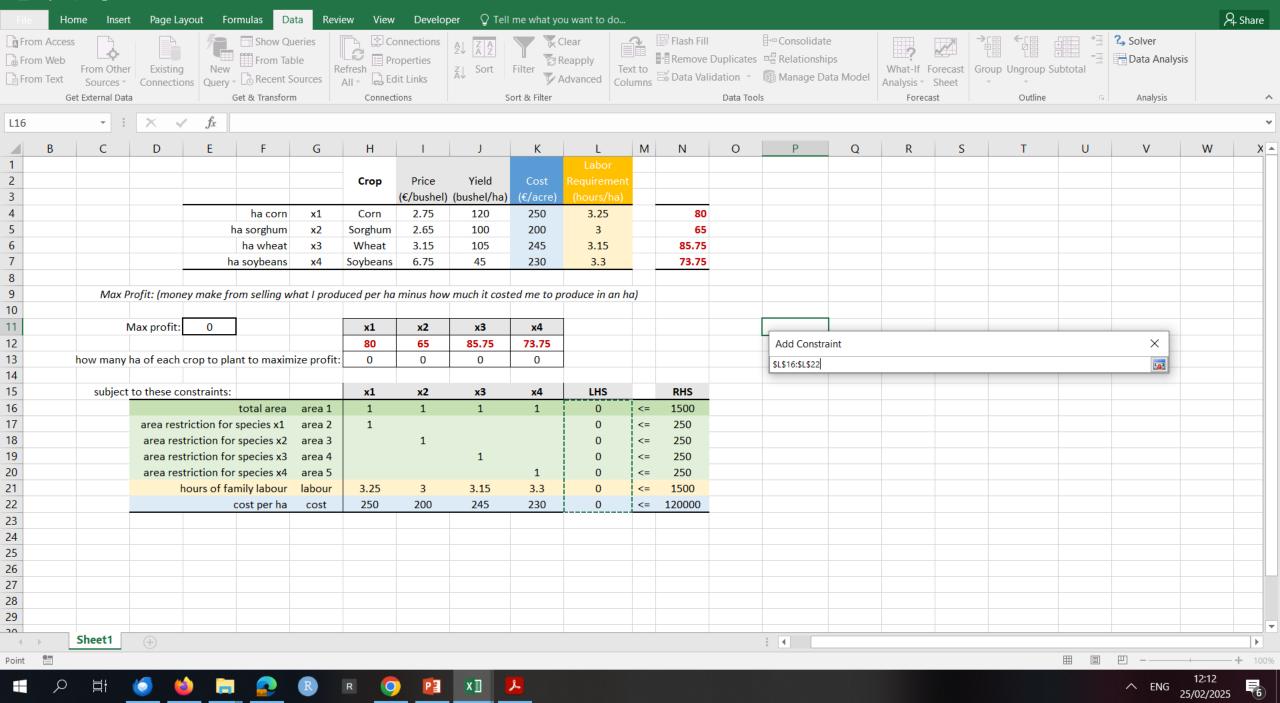
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Wheat	3.15	105	245	3.15
Soybeans	6.75	45	230	3.30

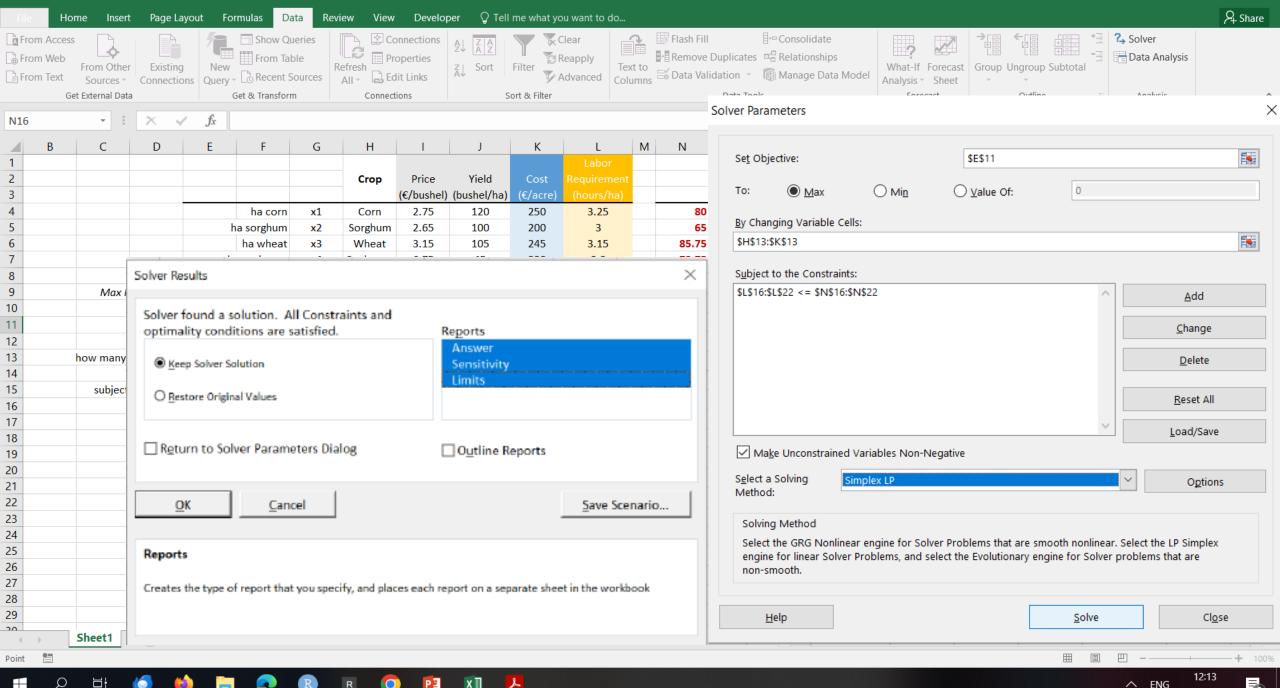
- 1. Formulate the problem as a linear program.
- 2. Solve the problem using the Excel Solver. What is the optimal solution to the problem?

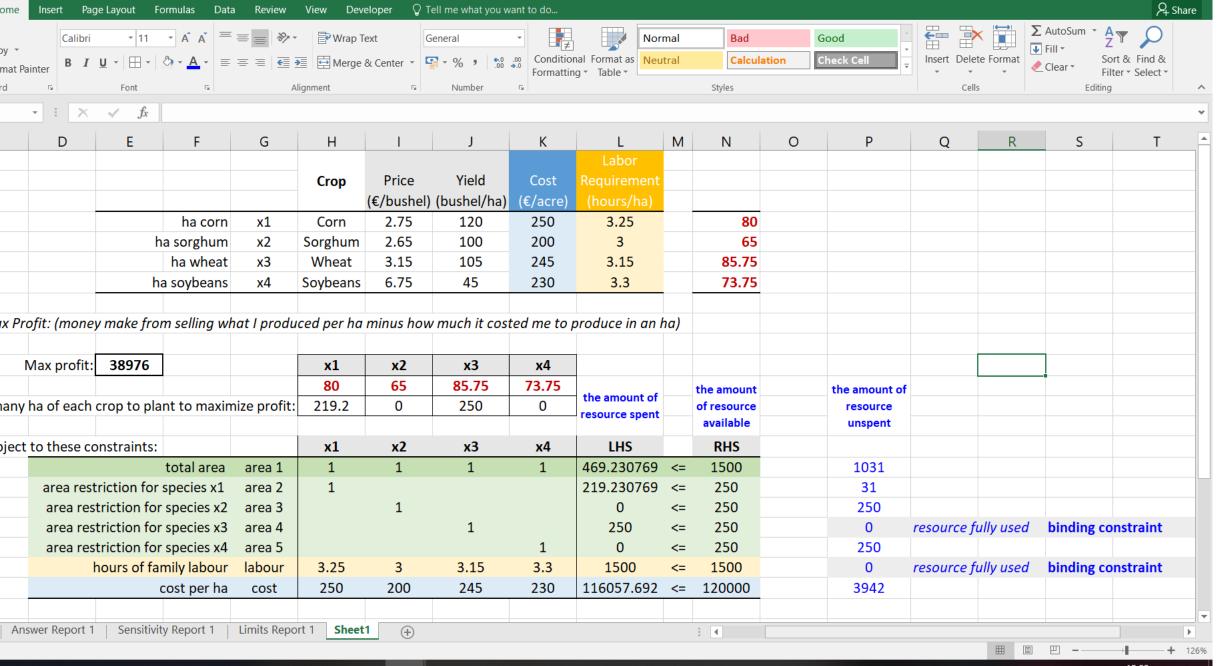
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### Question 2.

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- 1. Formulate the problem as a linear program.
- 2. Solve the problem using the Excel Solver. What is the optimal solution to the problem?

Once applied solver we find out the values of the decision variables (x1, x2, x3, x4) that maximize the profit of the farmer and the corresponding profit.

The optimal solution tells the farmer that to maximize profit she should plant:

219.2 ha of x1 (corn) 0 ha of x2 (sorghum) 250 ha of x3 (wheat) 0 ha of x4 (soybeans)

(x1, x2, x3, x4) = (219.2, 0, 250, 0) and that this would allow a profit of 38 976  $\in$ 



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- 1. Formulate the problem as a linear program.
- 2. Solve the problem using the Excel Solver. What is the optimal solution to the problem?
- 3. Which constraints are binding? How do you interpret each binding constraint?

Microsoft Excel 16.0 Answer Report Worksheet: [Book2]Sheet1

The Answer Report

Solver Engine

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Engine: Simplex LP

Iterations: 2 Subproblems: 0

Solution Time: 0.063 Seconds.

Report Created: 25/02/2025 12:17:53

Solver Options

Max Time Unlimited, Iterations Unlimited, Precision 0.000001, Use Automatic Scaling

Result: Solver found a solution. All Constraints and optimality conditions are satisfied.

Max Subproblems Unlimited, Max Integer Sols Unlimited, Integer Tolerance 1%, Assume NonNegative

The initial, optimal solutions (x1, x2, x3, x4), amount of (un)spent resources can be read across tables

Objective Cell (Max) Cell Original Value Final Value Name \$E\$11 Max profit: 0 38975.96154

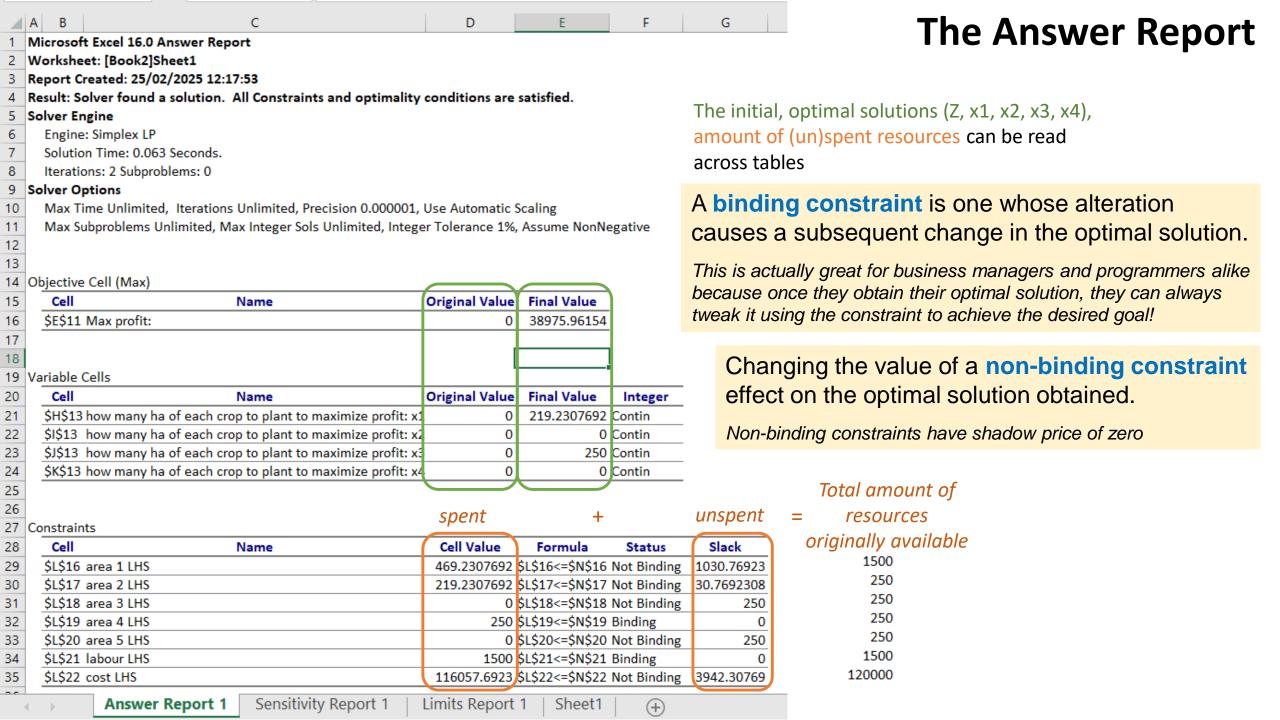
The **Objective Cell table** tells us the starting value of the objective function (Z) when Solver was applied and the optimal value after Solver

Variable Cells Cell Original Value Final Value Name Integer \$H\$13 how many ha of each crop to plant to maximize profit: x1 219.2307692 Contin \$I\$13 how many ha of each crop to plant to maximize profit: x2 0 Contin \$J\$13 how many ha of each crop to plant to maximize profit: x3 0 250 Contin \$K\$13 how many ha of each crop to plant to maximize profit: x4 0 Contin

The *Variables Cells table* shows the values of the decision variables (x1, x2, x3, x4) for the initial solution and the optimal solution

Constraints Slack Cell Value Cell Name Formula Status \$L\$16 area 1 LHS 469.2307692 \$L\$16<=\$N\$16 Not Binding 1030.76923 219.2307692 \$L\$17<=\$N\$17 Not Binding \$L\$17 area 2 LHS 30.7692308 \$L\$18 area 3 LHS 0 \$L\$18<=\$N\$18 Not Binding 250 \$L\$19 area 4 LHS 250 \$L\$19<=\$N\$19 Binding 0 \$L\$20 area 5 LHS 0 \$L\$20<=\$N\$20 Not Binding 250 \$L\$21 labour LHS 1500 \$L\$21<=\$N\$21 Binding \$L\$22 cost LHS 116057.6923 \$L\$22<=\$N\$22 Not Binding 3942.30769

The **Constraints** table provides information regarding the <u>restrictions</u> applied to each of the decision variables and <u>resources</u> (Formula), providing indication on which are the limiting resources - the binding constraints - that will have a positive shadow **price** (the table does not the shadow price value)





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- 3. Which constraints are binding? How do you interpret each binding constraint?

The binding constraints are those representing the resources that are fully used (area to plant wheat and labour time) and indicate that any change to these constraints will lead to a change in the optimal solution

$$x_3 \le 250$$

$$3.25x_1 + 3.00x_2 + 3.15x_3 + 3.30x_4 \le 1500$$



### Question 2.

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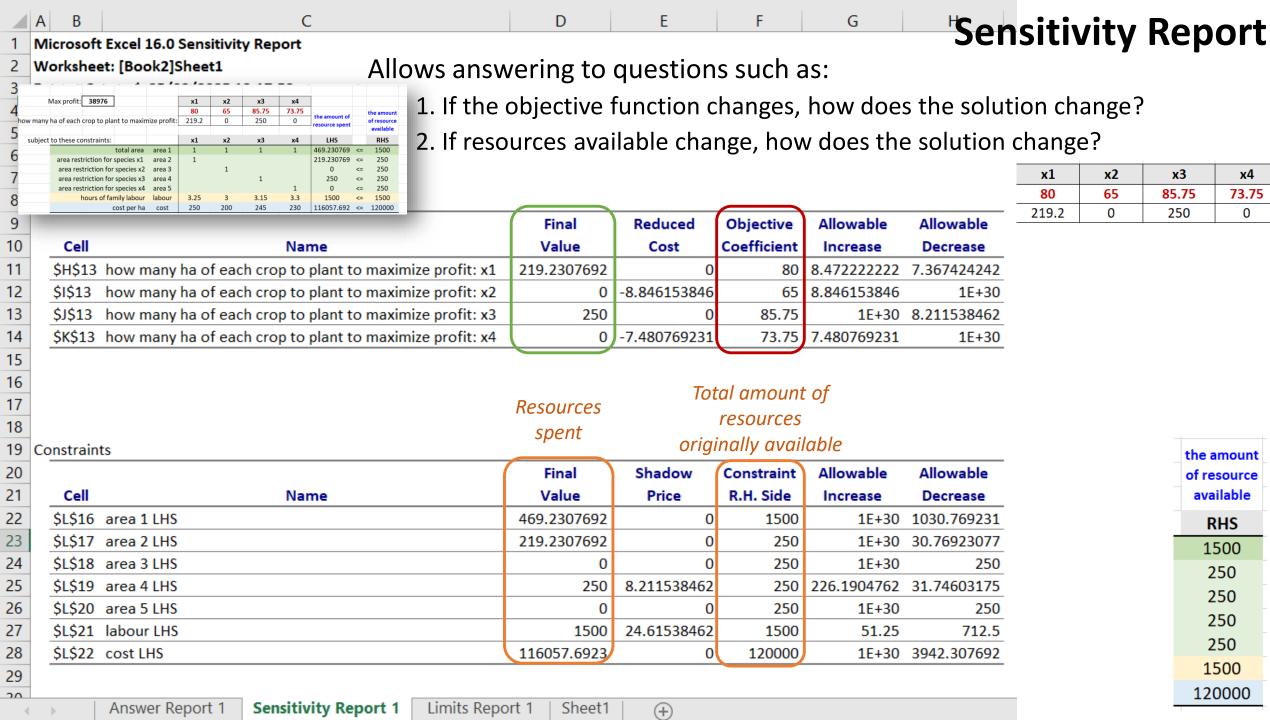
A farmer has the following resource endowments: 500 acres of land, 1500 hours of family labour and 120000 € of capital investment. She can use these resources to grow the following crops: corn, sorghum, wheat and soybeans. Any crop should not occupy more than 250 acres. Assume that the farmer works to maximize profit (revenue minus costs) from the production of these crops. She expects the following in terms of prices, crop yields, costs and labor requirements.

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- 4. By how much should sorghum's current profit per acre increase in order for the optimal solution to change? Sorghum's current profit per acre decrease would change the optimal solution?

#### Now we need to go into the output reports generated by solver:

- Answer report
- Sensitivity report



A B C D E F G Sensitivity Report Sensitivity Report

Allows answering to questions such as:

1. If the objective function changes, how does the solution change?

Maximize  $Z = 80x_1 + 65x_2 + 85.75x_3 + 73.75x_4$ 

ells					
		Reduced	Objective	Allowable	Allowable
Name	Value	Cost	Coefficient	Increase	Decrease
how many ha of each crop to plant to maximize profit: x1	219.2307692	0	80	8.47222222	7.367424242
how many ha of each crop to plant to maximize profit: x2	0	-8.846153846	65	8.846153846	1E+30
how many ha of each crop to plant to maximize profit: x3	250	0	85.75	1E+30	8.211538462
how many ha of each crop to plant to maximize profit: x4	0	-7.480769231	73.75	7.480769231	1E+30
	Name how many ha of each crop to plant to maximize profit: x1 how many ha of each crop to plant to maximize profit: x2 how many ha of each crop to plant to maximize profit: x3	Name  Value  219.2307692  Now many ha of each crop to plant to maximize profit: x1  Name  Name	Name  Name	Name  Name	Name  Name  Name  Nounce  Name  Nounce  Name  Nounce  Nounce  Name  Nounce  No

First, let us analyze the *Variable Cells* part of the table:

- The Final Value = *Optimal Solution*, thus replacing the final values (x1, X2, X3, X4) = (219.23, 0, 250, 0) in the objective function leads to:

MAX 
$$Z = 80*2.19.2 + 65*0 + 85.75*250 + 73.75*0 = 38 976$$
€

This tells the farmer that to maximize profit she should plant:

Worksheet: [Book2]Sheet1

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Report Created: 25/02/2025 12:17:53

Worksheet: [Book2]Sheet1

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Allows answering to questions such as:

1. If the objective function changes, how does the solution change?

Maximize 
$$Z = 80x_1 + 65x_2 + 85.75x_3 + 73.75x_4$$

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		Final	Reduced	Objective	Allowable	Allowable	interval	
Cell	Name	Value	Cost	Coefficient	Increase	Decrease		
\$H\$13	how many ha of each crop to plant to maximize profit: x1	219.2307692	0	80	8.472222222	7.367424242	72.6	88.5
\$I\$13	how many ha of each crop to plant to maximize profit: x2	0	-8.846153846	65	8.846153846	1E+30	INFINITY	73.8
\$J\$13	how many ha of each crop to plant to maximize profit: x3	250	0	85.75	1E+30	8.211538462	77.5	INFINITY
\$K\$13	how many ha of each crop to plant to maximize profit: x4	0	-7.480769231	73.75	7.480769231	1E+30	INFINITY	81.2

First, let us analyze the *Variable Cells* part of the table:

- The Final Value = Optimal Solution, thus replacing the final values (x1, X2, X3, X4) = (219.23, 0, 250, 0) in the objective function leads to:

MAX 
$$Z = 80*2.19.2 + 65*0 + 85.75*250 + 73.75*0 = 38 976$$
€

The *allowable increase* and *decrease* show how much the *coeff. of the objective function* can change before the *optimal solution* has to be altered

If the coeff of X1 increases up to 88.5 or drops down to 72.6 the optimal solution will hold = (219.23, 0, 250, 0)

MAX 
$$Z = 88.5*2.19.2 + 65*0 + 85.75*250 + 73.75*0 = 40833.3$$
 MAX  $Z = 72.6*2.19.2 + 65*0 + 85.75*250 + 73.75*0 = 22827.7$ 

#### Microsoft Excel 16.0 Sensitivity Report

### Worksheet: [Book2]Sheet1

Report Created: 25/02/2025 12:17:53

### Allows answering to questions such as:

1. If the objective function changes, how does the solution change?

Maximize 
$$Z = 80x_1 + 65x_2 + 85.75x_3 + 73.75x_4$$

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			Reduced	Objective	Allowable	Allowable
Cell	Name	Value	Cost	Coefficient	Increase	Decrease
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\$K\$13	how many ha of each crop to plant to maximize profit: x4	0	-7.480769231	73.75	7.480769231	1E+30

First, let us analyze the *Variable Cells* part of the table:

- The Final Value = Optimal Solution, thus replacing the final values (x1, X2, X3, X4) = (219.23, 0, 250, 0) in the objective function leads to:

MAX 
$$Z = 80*2.19.2 + 65*0 + 85.75*250 + 73.75*0 = 38976$$
€

The optimal solution tells the farmer:

"If you want to maximize profit DO NOT PLANT sorghum and soybeans"

The Reduced Cost measures the change in the objective function's value per unit increase in the decision variable's value.

What would happen if she planted 1 ha of sorghum (x2)? The profit would reduce to 38 967 € (38 976 - 8.85) The profit would reduce to 38 968.5 € (38976 - 7.48)What would happen if she planted 1 ha of soybeans (x4)?



### Question 2.

4. By how much should sorghum's current profit per acre increase in order for the optimal solution to change? Sorghum's current profit per acre decrease would change the optimal solution?

Variable C	Cells							
Cell	Name	Final Value	Reduced Cost	Objective Coefficient	Allowable Increase	Allowable Decrease		
\$H\$13	how many ha of each crop to plant to maximize profit: x1	219.2307692	0	80	8.472222222	7.367424242	72.6	88.5
\$1\$13	how many ha of each crop to plant to maximize profit: x2	0	-8.846153846	65	8.846153846	1E+30	INFINITY	73.8

Sorghum profit  $\Leftrightarrow$  coeficiente of x2 (set to 65)

How much can it increase to change the optimal solution?

If it <u>increases up</u> to the current value + the the allowable increase (73.8) <u>the optimal solution holds</u>

if the new <u>value > 65</u>+ 8.846 (the allowable increase) we'd be outsider the range (73.8) and the <u>optimal solution would NOT hold</u>

The profit can drop to zero that the solution will hold



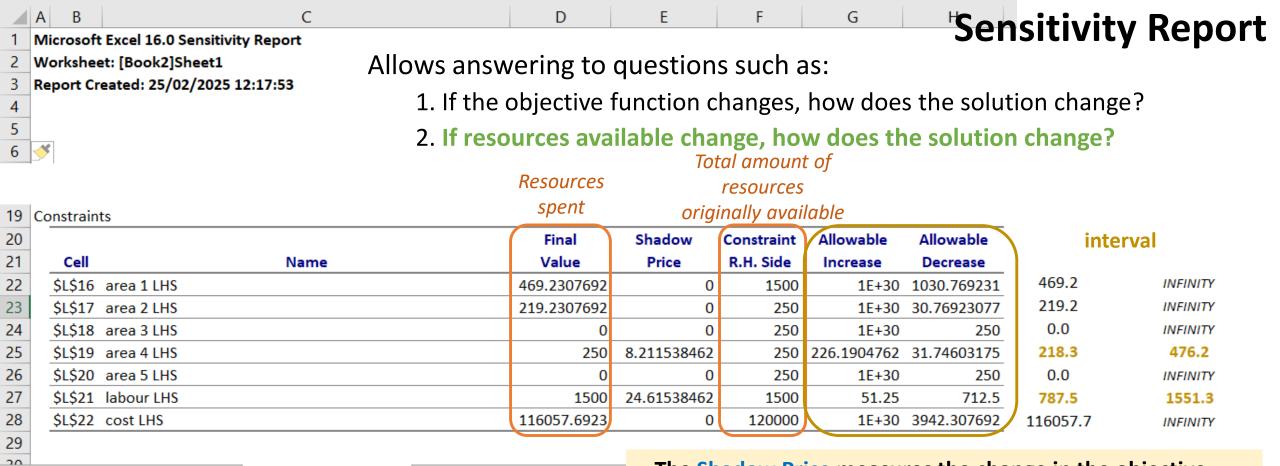
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Resources fully spent lead to **shadow price** > **zero** 

**Sensitivity Report 1** 

**Answer Report 1** 

Changes to the RHS of the constraints (*Total amount of resources originally available*):

**Limits Report 1** 

- if within the intervals set by the allowable decresase and increase will not change the optimal solution (but will affect the objective function value!)

The **Shadow Price** measures the change in the objective

function's value per unit increase in the constraint's bound.

- If outside the intervals set by the allowable decresase and increase will change the optimal solution and the objective function value

Sheet1

Microsoft Excel 16.0 Sensitivity Report Worksheet: [Book2]Sheet1

Report Created: 25/02/2025 12:17:53

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Allows answering to questions such as:

- 1. If the objective function changes, how does the solution change?
- 2. If resources available change, how does the solution change?

19	Constrain	ts								
20				Final	Shadow	Constraint	Allowable	Allowable	inte	erval
21	Cell		Name	Value	Price	R.H. Side	Increase	Decrease		
22	\$L\$16	area 1 LHS		469.2307692	0	1500	1E+30	1030.769231	469.2	INFINITY
23	\$L\$17	area 2 LHS		219.2307692	0	250	1E+30	30.76923077	219.2	INFINITY
24	\$L\$18	area 3 LHS		0	0	250	1E+30	250	0.0	INFINITY
25	\$L\$19	area 4 LHS		250	8.211538462	250	226.1904762	31.74603175	218.3	476.2
26	\$L\$20	area 5 LHS		0	0	250	1E+30	250	0.0	INFINITY
27	\$L\$21	labour LHS		1500	24.61538462	1500	51.25	712.5	787.5	1551.3
28	\$L\$22	cost LHS		116057.6923	0	120000	1E+30	3942.307692	116057.7	INFINITY
29										
20									_	
4	-	Answer Report 1	Sensitivity Report 1	Limits Report 1   Sheet1	(+)					

Constraints with a shadow price = zero are not worth changing because it will not have any impact on the objective function value

Changes on the RHS of constraints within the interval with a shadow price > zero will have impact on the objective function value. How much?

If the area available to plant wheat (constraint 4) increases in:

1 unit : 250 to 251 => Z\_new = 38 976 € + 1 \* 8.21 = 38 984

2 units: 250 to 252 => Z new = 38 976 € + 2 \* 8.21 = 38 992

226 units: 250 to 476 =>  $Z_new = 38 976 € + 226 * 8.21 = 40 832$ 

The same exercise can be achieved considering decreases in the RHS of constraint 4 of 31 units

- Microsoft Excel 16.0 Sensitivity Report
- Worksheet: [Book2]Sheet1

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- Report Created: 25/02/2025 12:17:53
- Allows answering to questions such as:
  - 1. If the objective function changes, how does the solution change?
  - 2. If resources available change, how does the solution change?

19	Constrain	ts								
20				Final	Shadow	Constraint	Allowable	Allowable	inte	rval
21	Cell		Name	Value	Price	R.H. Side	Increase	Decrease		
22	\$L\$16	area 1 LHS		469.2307692	0	1500	1E+30	1030.769231	469.2	INFINITY
23	\$L\$17	area 2 LHS		219.2307692	0	250	1E+30	30.76923077	219.2	INFINITY
24	\$L\$18	area 3 LHS		0	0	250	1E+30	250	0.0	INFINITY
25	\$L\$19	area 4 LHS		250	8.211538462	250	226.1904762	31.74603175	218.3	476.2
26	\$L\$20	area 5 LHS		0	0	250	1E+30	250	0.0	INFINITY
27	\$L\$21	labour LHS		1500	24.61538462	1500	51.25	712.5	787.5	1551.3
28	\$L\$22	cost LHS		116057.6923	0	120000	1E+30	3942.307692	116057.7	INFINITY
29										
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4	-	Answer Report 1	Sensitivity Report 1	Limits Report 1   Sheet1	(+)					

Constraints with a shadow price = zero are not worth changing because it will not have any impact on the objective function value

Changes on the RHS of constraints within the interval with a shadow price > zero will have impact on the objective function value. How much? The same exercise

If the family labour time available for agriculture (constraint 6) decreases in:

1 unit: 1500 to 1499 => Z new = 38 976 € -1 \* **24.62** = 38 951 Z new = 38 976 € -2 units: 1500 to 1498 => 2 \* **24.62** = 38 927

**712.5** units: 1500 to **1449** => Z\_new = 38 976 € - **712.5** \* **24.62** = 21 438

can be achieved considering increases in the **RHS** of constraint 6 of 51 units

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# Allows answering to questions such as:

1. If the objective function changes, how does the solution change?

**Sensitivity Report** 

2. If resources available change, how does the solution change?

9	Constrain	ts								
0				Final	Shadow	Constraint	Allowable	Allowable	inte	rval
1	Cell		Name	Value	Price	R.H. Side	Increase	Decrease		
2	\$L\$16	area 1 LHS		469.2307692	0	1500	1E+30	1030.769231	469.2	INFINITY
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4	\$L\$18	area 3 LHS		0	0	250	1E+30	250	0.0	INFINITY
5	\$L\$19	area 4 LHS		250	8.211538462	250	226.1904762	31.74603175	218.3	476.2
6	\$L\$20	area 5 LHS		0	0	250	1E+30	250	0.0	INFINITY
7	\$L\$21	labour LHS		1500	24.61538462	1500	51.25	712.5	787.5	1551.3
8	\$L\$22	cost LHS		116057.6923	0	120000	1E+30	3942.307692	116057.7	INFINITY
9										
^				11 11 0 14 101 14	1 0					
4		Answer Report 1	Sensitivity Report 1	Limits Report 1   Sheet1	+					

constraints with a
shadow price = zero
are not worth changing
because it will not have
any impact on the
objective function
value

The impact of changes on the RHS of constraints that fall **outside** the interval can only be determined by solving the problem again!



### Question 2.

#### Test - 25 May 2016

A farmer has the following resource endowments: 500 acres of land, 1500 hours of family labour and 120000 € of capital investment. She can use these resources to grow the following crops: corn, sorghum, wheat and soybeans. Any crop should not occupy more than 250 acres. Assume that the farmer works to maximize profit (revenue minus costs) from the production of these crops. She expects the following in terms of prices, crop yields, costs and labor requirements.

	Price	Yield	Cost	Labor Requirement
$\operatorname{Crop}$	(€/bushel)	(bushel/acre)	(€/acre)	(hours/acre)
Corn	2.75	120	250	3.25
Sorghum	2.65	100	200	3.00
Wheat	3.15	105	245	3.15
Soybeans	6.75	45	230	3.30

- 1. Formulate the problem as a linear program.
- 2. Solve the problem using the Excel Solver. What is the optimal solution to the problem?
- 3. Which constraints are binding? How do you interpret each binding constraint?
- 4. By how much should sorghum's current profit per acre increase in order for the optimal solution to change? Sorghum's current profit per acre decrease would change the optimal solution?
- 5. What is the shadow price for each constraint? How do you interpret this value?

The Shadow Price is the impact that one unitary change in the RHS of any given constraint will have in the objective function value. This is only true as long as changes on the RHS of constraints remain within the interval determined by the allowable increases and decreases



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- 6. What is the range of feasibility for the maximum number of hours of family labour with respect to the shadow price? How do you interpret this range?



### Question 2.

6. What is the range of feasibility for the maximum number of hours of family labour with respect to the shadow price? How do you interpret this range?

The range of feasibility with respect to the maximum number of hours sets the upper limit at 1551.3 considering increases in labour time that can reach a maximum of 51.25 hours with a immediate consequence in the objective function value. Thus, an increase of 51.25 : from 1500 to 1551.25 =>

Z\_new = 38 976 € + **51.25** \* **24.62** = 40 238 € (profit increases, original values 38 976 €)

26	\$L\$20 area 5 LHS	0	0	250	1E+30	250	0.0	INFINITY
27	\$L\$21 labour LHS	1500	24.61538462	1500	51.25	712.5	787.5	1551.3
28	\$L\$22 cost LHS	116057.6923	0	120000	1E+30 39	3942.307692	116057.7	INFINITY

However, na increase of 52 hours would already fall outsider the range of feasibility making impossible to use the shadow price to determine the impact on the objective function and forcing the problema to be solved again.



### Question 2.

#### Test - 25 May 2016

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- 5. What is the shadow price for each constraint? How do you interpret this value?
- 6. What is the range of feasibility for the maximum number of hours of family labour with respect to the shadow price? How do you interpret this range?
- 7. How much the profit would change if one acre of soybeans were forced into the current optimal solution?



# Question 2.

7. How much the profit would change if one acre of soybeans were forced into the current optimal solution?

Imposing the plantation of 1 ha of soybeans will have a negative impact of 7.48 € in the final profit value. Thus, the increase of x4 frm 0 to 1 ha

Z\_new = 38 976 € - **7.48** = **38 968.5** € (profit decreases, original values 38 976 €)

and the control of th							
		Final	Final Reduced		Objective	Allowable	Allowable
Cell	Name	Value		Cost	Coefficient	Increase	Decrease
\$H\$13	how many ha of each crop to plant to maximize profit: x1	219.2307692		0	80	8.47222222	7.367424242
\$I\$13	how many ha of each crop to plant to maximize profit: x2	0	-8.	846153846	65	8.846153846	1E+30
\$J\$13	how many ha of each crop to plant to maximize profit: x3	250		0	85.75	1E+30	8.211538462
\$K\$13	how many ha of each crop to plant to maximize profit: x4	0	-7.	480769231	73.75	7.480769231	1E+30



### Question 7.

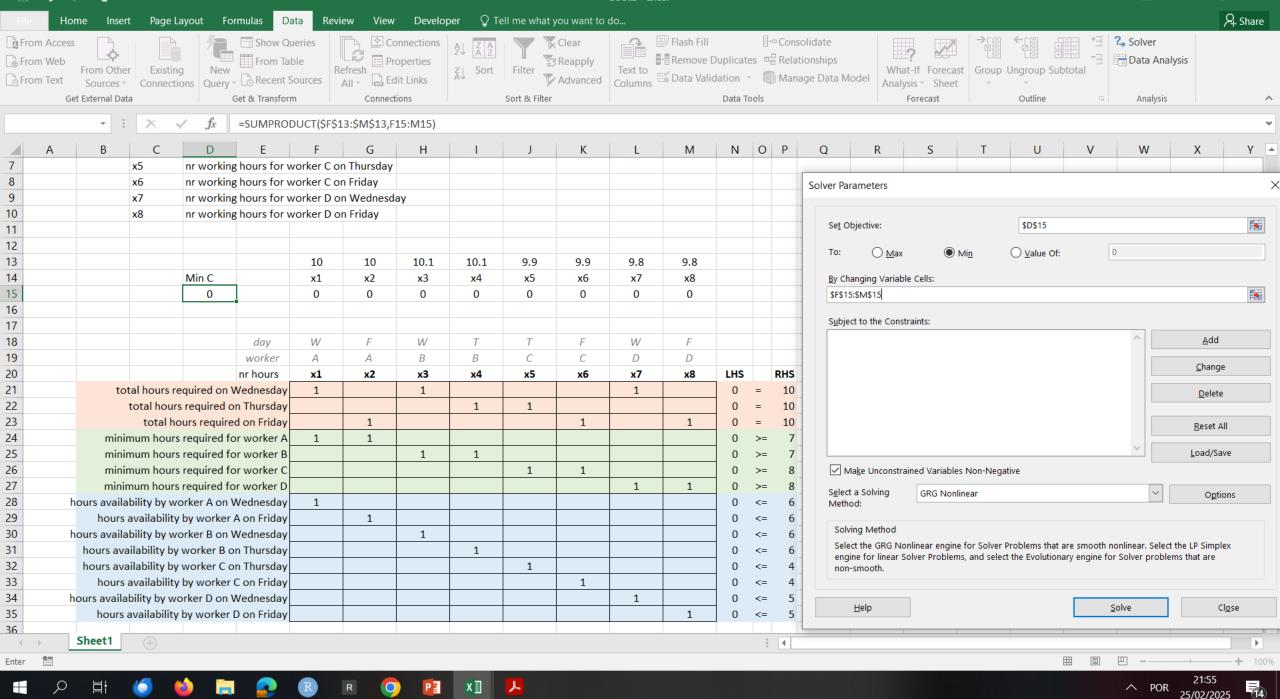
#### Exam - 17 June 2022

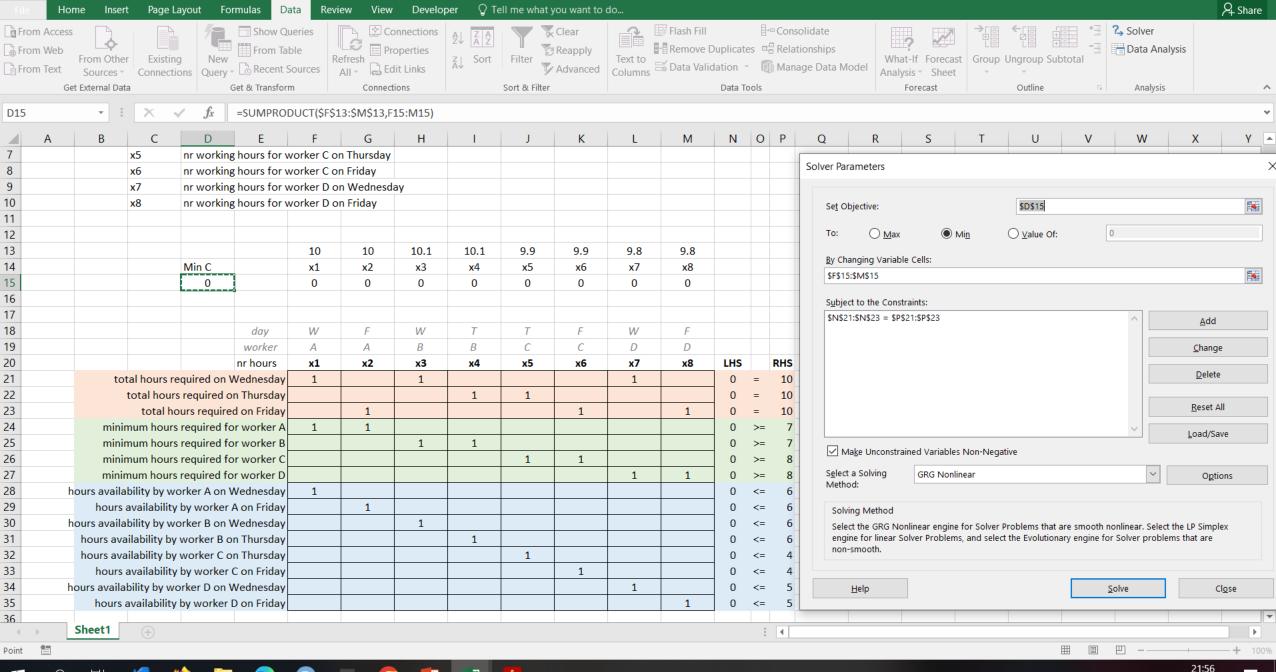
A certain university maintains a powerful mainframe computer for research use. There are four operators (two graduate students and two undergraduate students) to operate and maintain the computer, as well as to perform some programming services, from Wethesday to Friday (in the other days the computer is to be operated by staff outside the university). They all have different wage rates because of differences in their experience with computers and in their programming ability. Table 1 shows their wage rates, along with the maximum number of hours that each can work each day. Each operator is guaranteed a certain minimum number of hours per week that will maintain an adequate knowledge of the operation. This level is set arbitrarily at 7 hours per week for the graduate students (A and B) and 8 hours per week for the undergraduate students (C and D).

		Maximum Hours of Availability				
Operators	Wage Rate	Wednesday	Thursday	Friday		
	(€/hour)					
A	10.00	6	0	6		
В	10.10	6	6	0		
C	9.90	0	4	4		
D	9.80	5	0	5		

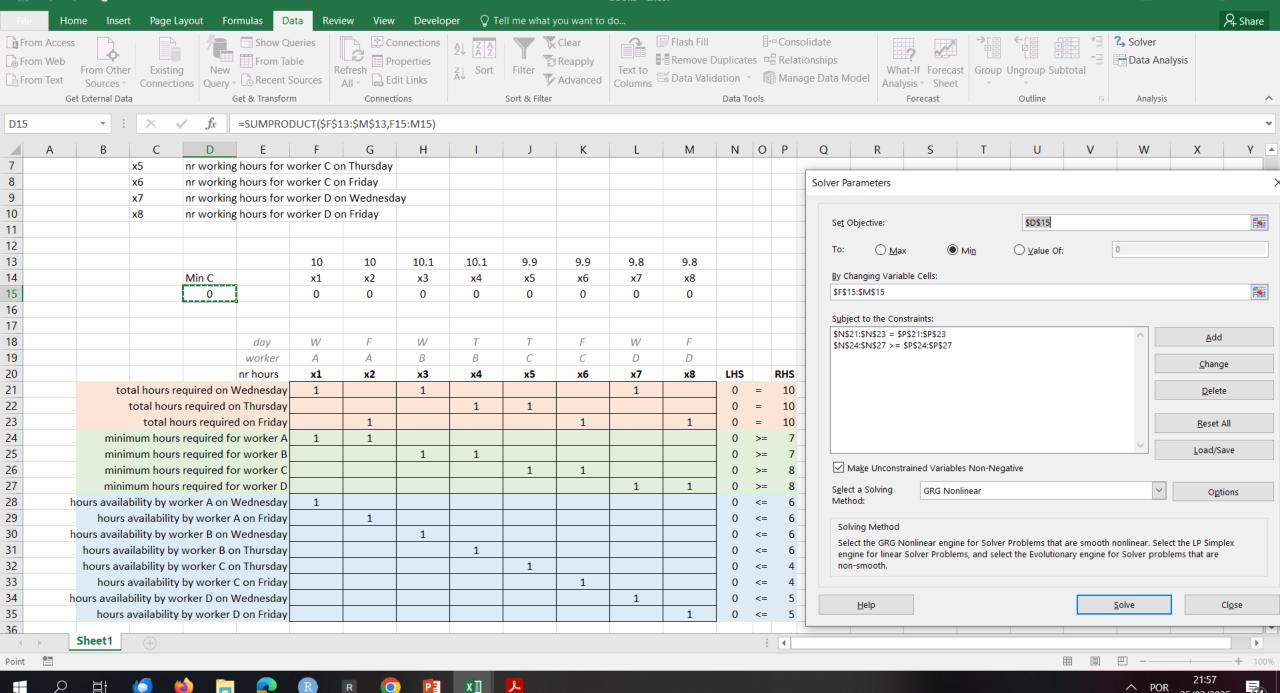
The computer facility is to be open for operation from 8 A.M. to 6 P.M. every day. The director of the computer facility wishes to determine the number of hours she should assign to each operator on each day in order to minimize cost.

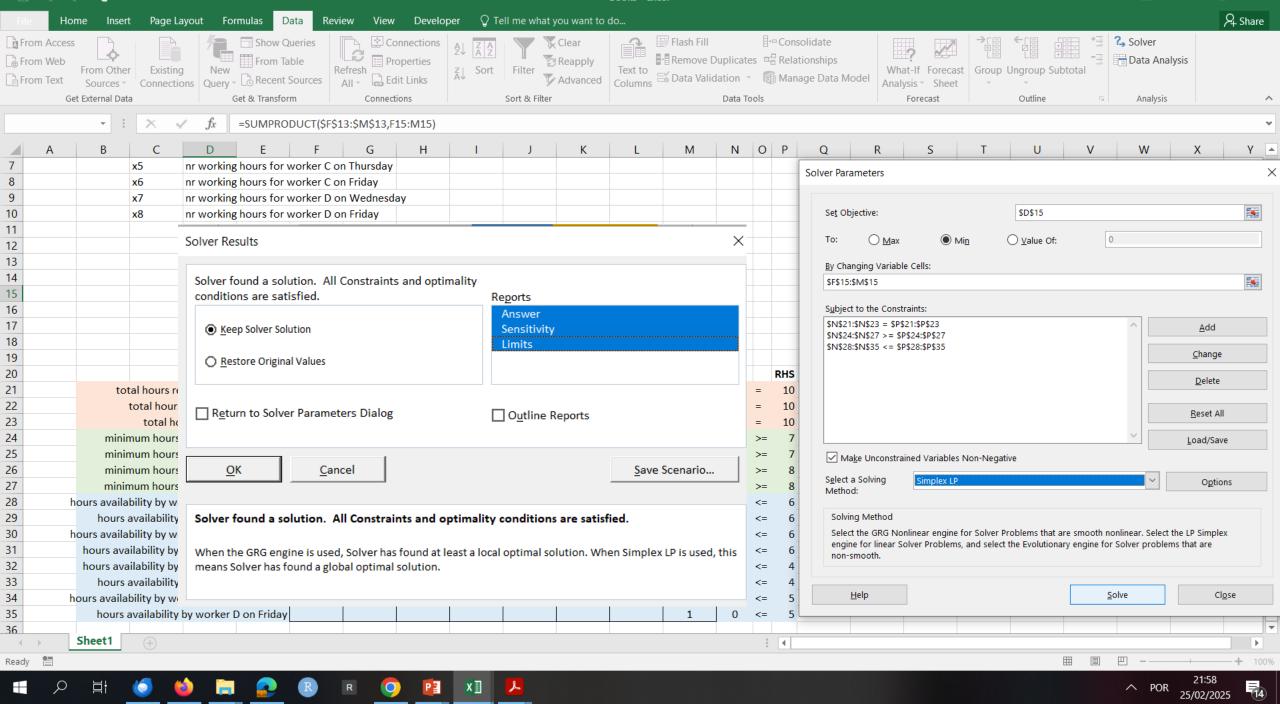
- 1. Formulate a linear programming model for this problem.
- Determine a feasible solution.

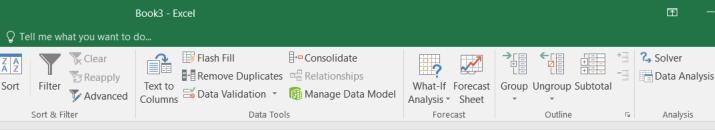


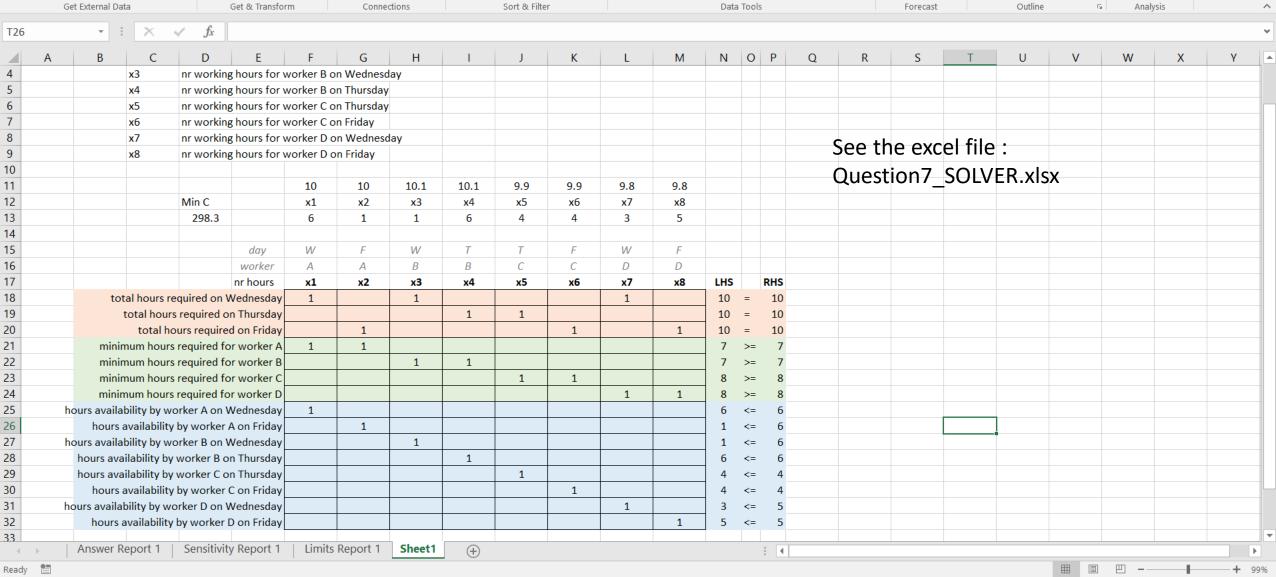


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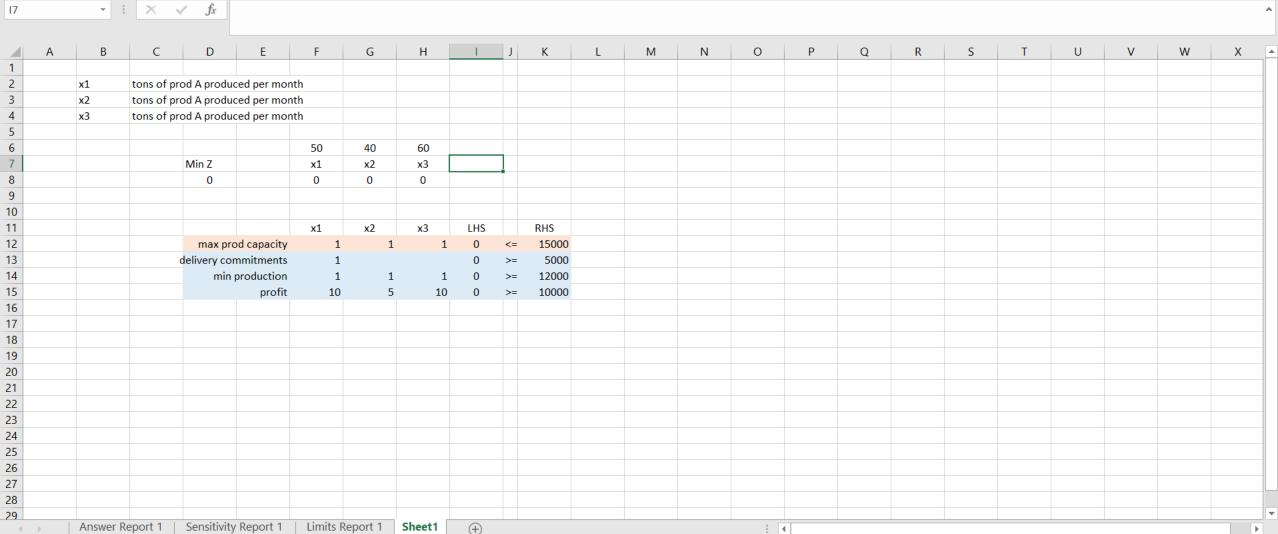


### Question 8.

#### Exam - 30 June 2022

A company produces three types of forest products, A, B and C. Each ton of product A, B and C generates 50, 40 and 60 units of toxic waste and generate a profit of 10, 5 and 10 euros, respectively. The company has the capacity to produce up to 15 thousand tons of products per month. Commitments already made oblige the company to deliver to a certain customer 5 thousand tons of product A each month. One intends to determine the **monthly production plan** that generates the minimum amount of toxic waste with a monthly profit of at least 100 thousand euros and a monthly production of never less than 80% of the maximum production capacity of the company.

- 1. Formulate a linear programming model for this problem.
- 2. Consider that 12 thousand tons of products are produced each month, generating a profit of 100 thousand euros and that the monthly production of product A is 8 thousand tons. Indicate the quantities of products B and C produced and the amount of toxic waste generated.



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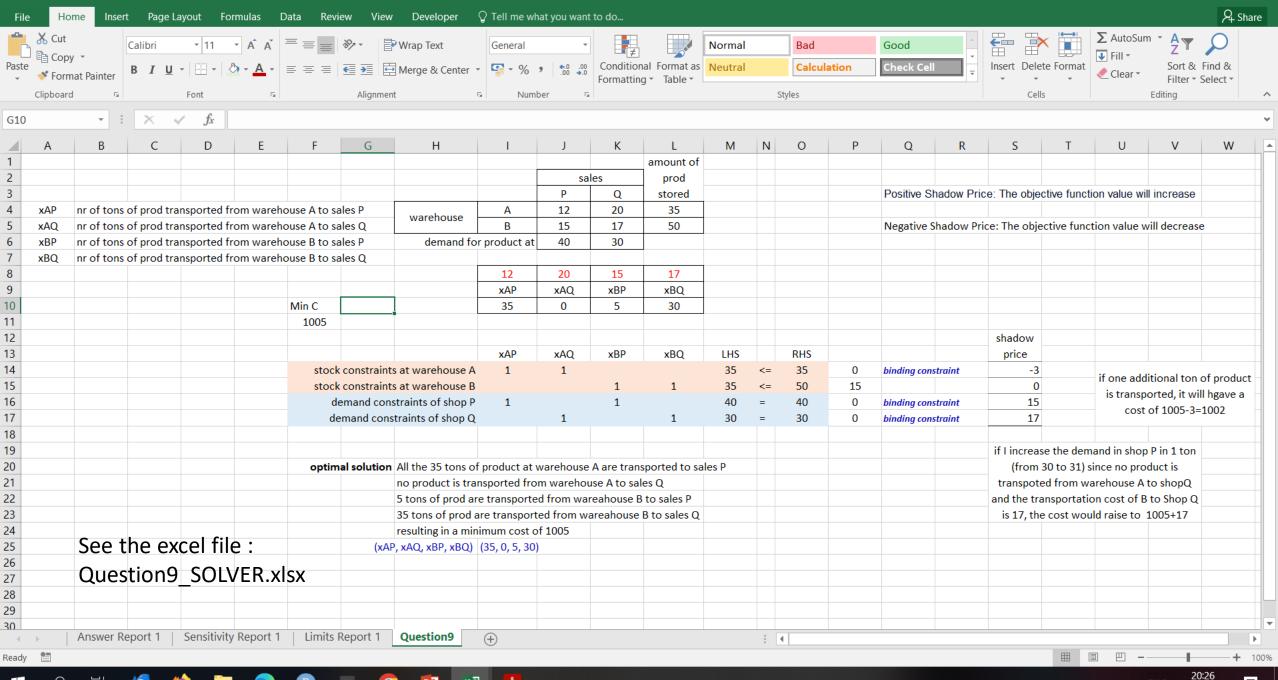
### Question 9.

#### Test - 29 March 2023

A company transports a certain product from the warehouses A and B to the sales centers P and Q. The amounts of product in A and B are 35 and 50 tons, respectively. The demands for P and Q are 40 and 30 tons, respectively. The cost, in euros, of transporting 1 ton of product from each warehouse to each sale center is indicated in the following table.

	Р	Q
A	12	20
В	15	17

The company wants to establish a supply plan that meets the minimum cost. Formulate the problem in linear programming.





### Question 11.

#### Exam - 16 June 2023

A student on a tight budget wishes to plan a daily diet which will minimize his food expenditure while maintaining minimum nutritional requirements, according to the Recommended Daily Allowance (RDA). The student wants to plan his menu fom the following goods: hamburgers, hot dogs, salad, chicken, pizza, carrots and cookies. The dietary information and cost of these foods is as follows:

Nutrient	Hamburger	$\operatorname{Hot} \operatorname{dog}$	Salad	Chicken	Pizza	Carrots	Cookies	RDA
Calories (cal/kg)	4400	4200	1000	1400	5000	600	5200	5000 cal
Calcium (mg/kg)	200	400	800	600	950	800	300	160  mg
Protein (mg/kg)	100	140	40	90	70	50	20	50  mg
Iron (mg/kg)	50	30	60	20	10	30	40	30  mg
Cost (€/kg)	5.0	4.0	3.5	6.0	10.0	4.5	7.0	

Furthermore, assume that the student wants to eat 125 grams of cookies each day and will eat at most 250 grams of carrots per day.

Formulate the problem as a linear program and indicate a feasible daily diet with the corresponding cost.

