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|---|--|
| 1) $(k)' = 0$ | 10) $(\operatorname{tg} f)' = \sec^2 f \cdot f'$ |
| 2) $(f^\alpha)' = \alpha \cdot f^{\alpha-1} \cdot f', \quad \alpha \in \mathbb{R}$ | $(\sec f = \frac{1}{\cos f})$ |
| 3) $(e^f)' = e^f \cdot f'$ | 11) $(\operatorname{cotg} f)' = -\operatorname{cosec}^2 f \cdot f'$ |
| 4) $(a^f)' = a^f \cdot f' \cdot \ln a, \quad a \in \mathbb{R}^+$ | $(\operatorname{cotg} f = \frac{1}{\operatorname{tg} f} \text{ e } \operatorname{cosec} f = \frac{1}{\sin f})$ |
| 5) $(\ln f)' = \frac{f'}{f}$ | 12) $(\sec f)' = \sec f \cdot \operatorname{tg} f \cdot f'$ |
| 6) $(\log_a f)' = \frac{f'}{f \cdot \ln a}, \quad a \in \mathbb{R}^+ \setminus \{1\}$ | 13) $(\operatorname{cosec} f)' = -\operatorname{cosec} f \cdot \operatorname{cotg} f \cdot f'$ |
| 7) $(f^g)' = g \cdot f^{g-1} \cdot f' + f^g \cdot \ln f \cdot g', \quad f > 0$ $(f^g = e^{g \ln f})$ | 14) $(\arcsin f)' = \frac{f'}{\sqrt{1-f^2}}$ |
| 8) $(\sin f)' = \cos f \cdot f'$ | 15) $(\arccos f)' = \frac{-f'}{\sqrt{1-f^2}}$ |
| 9) $(\cos f)' = -\sin f \cdot f'$ | 16) $(\operatorname{arctg} f)' = \frac{f'}{1+f^2}$ |

Tabela 1.1: Derivadas de algumas funções elementares.

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| 1) $(f + g)' = f' + g'$ |
| 2) $(\alpha f)' = \alpha f', \quad \alpha \in \mathbb{R}$ |
| 3) $(fg)' = f'g + fg'$ |
| 4) $\left(\frac{f}{g}\right)' = \frac{f'g - fg'}{g^2}$ |
| 5) $(g \circ f)'(x) = g'[f(x)] f'(x)$ |

Tabela 1.2: Regras de derivação.

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| 1) $\sin^2 x + \cos^2 x = 1$ | 3) $1 + \operatorname{cotg}^2 x = \operatorname{cosec}^2 x$ |
| 2) $1 + \operatorname{tg}^2 x = \sec^2 x$ | 5) $\cos(x+y) = \cos x \cos y - \sin x \sin y$ |
| 4) $\sin(x+y) = \sin x \cos y + \sin y \cos x$ | 7) $\cos(x-y) = \cos x \cos y + \sin x \sin y$ |
| 6) $\sin(x-y) = \sin x \cos y - \sin y \cos x$ | 9) $\cos 2x = \cos^2 x - \sin^2 x$ |
| 8) $\sin 2x = 2 \sin x \cos x$ | 11) $\cos^2 x = \frac{1}{2}(1 + \cos 2x)$ |
| 10) $\sin^2 x = \frac{1}{2}(1 - \cos 2x)$ | 13) $\cos x = \frac{1 - \operatorname{tg}^2 x/2}{1 + \operatorname{tg}^2 x/2}$ |
| 12) $\sin x = \frac{2 \operatorname{tg} x/2}{1 + \operatorname{tg}^2 x/2}$ | 16) $\sin mx \cos nx = \frac{1}{2}[\sin(m+n)x + \sin(m-n)x]$ |
| 14) $\sin mx \cos nx = \frac{1}{2}[\cos(m+n)x + \cos(m-n)x]$ | |
| 15) $\cos mx \cos nx = \frac{1}{2}[\cos(m+n)x + \cos(m-n)x]$ | |

Tabela 2.4: Fórmulas trigonométricas que poderão ser úteis na primitivação.

| Função a primitivar | Primitiva |
|---|---|
| 1) $k, k \in \mathbb{R}$ | kx |
| 2) $f^\alpha \cdot f', \alpha \in \mathbb{R} \setminus \{-1\}$ | $\frac{f^{\alpha+1}}{\alpha+1}$ |
| $x^\alpha, \alpha \in \mathbb{R} \setminus \{-1\}$ | $\frac{x^{\alpha+1}}{\alpha+1}$ |
| 3) $\frac{f'}{f}$ | $\ln f $ |
| $\frac{1}{x}$ | $\ln x $ |
| 4) $\sin f \cdot f'$ | $-\cos f$ |
| 5) $\cos f \cdot f'$ | $\sin f$ |
| 6) $\operatorname{tg} f \cdot f'$ | $-\ln \cos f $ |
| 7) $\operatorname{cotg} f \cdot f'$ | $\ln \sin f $ |
| 8) $\operatorname{sec}^2 f \cdot f'$ | $\operatorname{tg} f$ |
| 9) $\operatorname{cosec}^2 f \cdot f'$ | $-\operatorname{cotg} f$ |
| 10) $\operatorname{sec} f \cdot f'$ | $\ln \sec f + \operatorname{tg} f $ |
| 11) $\operatorname{cosec} f \cdot f'$ | $\ln \operatorname{cosec} f - \operatorname{cotg} f $ |
| 12) $\sec f \cdot \operatorname{tg} f \cdot f'$ | $\sec f$ |
| 13) $\operatorname{cosec} f \cdot \operatorname{cotg} f \cdot f'$ | $-\operatorname{cosec} f$ |
| 14) $a^f \cdot f', a \in \mathbb{R}^+ \setminus \{1\}$ | $\frac{a^f}{\ln a}$ |
| 15) $e^f \cdot f'$ | e^f |
| 16) $\frac{f'}{\sqrt{1-f^2}}$ | $\arcsin f$ |
| 17) $\frac{-f'}{\sqrt{1-f^2}}$ | $\arccos f$ |
| 18) $\frac{f'}{1+f^2}$ | $\operatorname{arctg} f$ |

Tabela 2.1: Primitivas de algumas funções.

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| 1) $P(f+g) = Pf + Pg$ |
| 2) $P\lambda f = \lambda Pf, \text{ com } \lambda \in \mathbb{R}$ |
| 3) $P(fg) = Fg - P(Fg'), \text{ com } F = Pf$ |
| 4) $Pf(x) = P(f(\varphi(t))\varphi'(t)), \text{ com } x = \varphi(t)$ |

Tabela 2.3: Propriedades das primitivas.