

RLS - Modelo Linear: $Y_i = \beta_0 + \beta_1 x_i + \epsilon_i, i = 1, \dots, n$

$$\hat{Y}_i = \hat{\beta}_0 + \hat{\beta}_1 x_i = \bar{Y} + \hat{\beta}_1(x_i - \bar{x})$$

$\epsilon_i \cap \mathcal{N}(0, \sigma^2)$ para $\forall i = 1, \dots, n$ e $\{\epsilon_i\}_{i=1}^n$ v.a. independentes

Parâmetro	Estimador	Distribuição associada	Estimativa
σ^2	$\widehat{\sigma}^2 = QMRE = \frac{SQRE}{n-2} = \frac{\sum_{i=1}^n (Y_i - \hat{Y}_i)^2}{n-2}$	$\frac{SQRE}{\sigma^2} \cap \chi^2_{(n-2)}$	$QMRE = \frac{(n-1)s_e^2}{n-2}$
β_1	$\hat{\beta}_1 = \frac{Cov_{xY}}{s_x^2} = \sum_{i=1}^n c_i Y_i, \quad c_i = \frac{x_i - \bar{x}}{(n-1)s_x^2}$	$\frac{\hat{\beta}_1 - \beta_1}{\sigma_{\hat{\beta}_1}} \cap \mathcal{N}(0,1), \quad \sigma_{\hat{\beta}_1}^2 = \frac{\sigma^2}{(n-1)s_x^2}$ $\frac{\hat{\beta}_1 - \beta_1}{\hat{\sigma}_{\hat{\beta}_1}} \cap t_{(n-2)}, \quad \hat{\sigma}_{\hat{\beta}_1}^2 = \frac{QMRE}{(n-1)s_x^2}$	$b_1 = \frac{cov(x,y)}{s_x^2}$
β_0	$\hat{\beta}_0 = \bar{Y} - \hat{\beta}_1 \bar{x} = \sum_{i=1}^n d_i Y_i, \quad d_i = \frac{1}{n} - \frac{(x_i - \bar{x})\bar{x}}{(n-1)s_x^2}$	$\frac{\hat{\beta}_0 - \beta_0}{\sigma_{\hat{\beta}_0}} \cap \mathcal{N}(0,1), \quad \sigma_{\hat{\beta}_0}^2 = \sigma^2 \left[\frac{1}{n} + \frac{\bar{x}^2}{(n-1)s_x^2} \right]$ $\frac{\hat{\beta}_0 - \beta_0}{\hat{\sigma}_{\hat{\beta}_0}} \cap t_{(n-2)}, \quad \hat{\sigma}_{\hat{\beta}_0}^2 = QMRE \left[\frac{1}{n} + \frac{\bar{x}^2}{(n-1)s_x^2} \right]$	$b_0 = \bar{y} - b_1 \bar{x}$
$\mu_{Y x} = E[Y X=x] = \beta_0 + \beta_1 x$	$\hat{\mu}_{Y x} = \hat{\beta}_0 + \hat{\beta}_1 x$	$\frac{\hat{\mu}_{Y x} - \mu_{Y x}}{\hat{\sigma}_{\hat{\mu}}} \cap t_{(n-2)}, \quad \hat{\sigma}_{\hat{\mu}}^2 = QMRE \left[\frac{1}{n} + \frac{(x - \bar{x})^2}{(n-1)s_x^2} \right]$ Nota: IP para $Y = \beta_0 + \beta_1 x + \epsilon$ tem $\widehat{\sigma}_{ind}^2 = QMRE \left[1 + \frac{1}{n} + \frac{(x - \bar{x})^2}{(n-1)s_x^2} \right]$	$\hat{y} = b_0 + b_1 x$
\mathcal{R}^2	$R^2 = \frac{SQR}{SQT} = \frac{\sum_{i=1}^n (\hat{Y}_i - \bar{Y})^2}{\sum_{i=1}^n (Y_i - \bar{Y})^2}$	$F = \frac{QMR}{QMRE} \cap F_{(1,n-2)} \quad \text{se } \beta_1 = 0$ $F = (n-2) \frac{R^2}{1-R^2}$	$R^2 = \frac{SQR}{SQT} = \frac{\sum_{i=1}^n (\hat{y}_i - \bar{y})^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$